| Question |  | Answer | $\begin{gathered} \hline \text { Marks } \\ \hline \text { M1 } \end{gathered}$ | $\begin{array}{\|c\|} \hline \text { AO } \\ \hline 1.1 \mathrm{a} \\ \hline \end{array}$ | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (a) | (i) | $x^{2}+(m x+2)^{2}-10 x-14(m x+2)+64=$ <br> 0 $\begin{aligned} & x^{2}+m^{2} x^{2}+4 m x+4-10 x-14 m x-28+ \\ & 0 \\ & \left(m^{2}+1\right) x^{2}-10(m+1) x+40=0 \end{aligned}$ <br> A.G. | A1 | $1.1 \mathrm{a}$ $1.1$ | Substitute eqn of tangent into eqn of circle <br> Expand and tidy to given answer, including ' $=0$ ' in final answer | Could work backwards, eliminating $m$ to obtain equation of circle <br> AG so unsimplified expansion needs to be seen |
|  | (ii) | $\begin{aligned} & 100(m+1)^{2}-160\left(m^{2}+1\right)=0 \\ & 60 m^{2}-200 m+60=0 \\ & (3 m-1)(m-3)=0 \\ & m=3, m=\frac{1}{3} \\ & y=3 x+2 \end{aligned}$ | $\begin{gathered} \text { M1* } \\ \text { A1 } \\ \text { M1d* } \\ \text { A1 } \\ \\ {[4]} \end{gathered}$ | $\begin{gathered} \hline \text { 3.1a } \\ 1.1 \\ \text { 1.1a } \\ 1.1 \end{gathered}$ | Use $b^{2}-4 a c=0$ <br> Obtain correct equation <br> Attempt to solve quadratic <br> Obtain correct equation | M1 only awarded when ' $=0$ ' soi Any correct 3 term equation DR so method for solving the quadratic must be shown <br> SC B1for correct equation if roots not justified <br> A0 if second equation also given <br> OR (for first 2 marks) <br> M1 - Attempt two equations in $m$ and $x$ (eg use lengths and gradients) and eliminate one variable <br> A1 - correct quadratic in $m$ or $x$ |
| (b) |  | $\begin{aligned} & \text { radius }=\sqrt{10}, P C=5 \sqrt{2}, \\ & P A=P B=2 \sqrt{10}, A B=4 \sqrt{2} \\ & \tan \left(\frac{1}{2} A P B\right)=\frac{1}{2} \\ & \tan A P B=\frac{1}{1-\frac{1}{4}} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \end{aligned}$ | $\begin{gathered} 3.1 \mathrm{a} \\ 1.1 \\ 3.1 \mathrm{a} \end{gathered}$ | Attempt (at least 2) useful lengths <br> Obtain a correct related trig ratio Attempt tan APB | NB points of intersection are $(2,8)$ and (6, 4) $\cos A P B=\frac{3}{5}$, from cosine rule DR so need to see use of identity or relevant triangle to find $\tan A P B$ |


| Question | Answer | Marks | AO | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\tan A P B=\frac{4}{3}$ | A1 <br> [4] | 1.1 | Obtain $\frac{4}{3}$ | From explicit, exact, working |
|  |  |  |  |  | OR <br> M2 - attempt $\frac{ \pm m \pm n}{1 \pm m n}$ with their values for $m$ and $n$ <br> A1FT - correct $\frac{m-n}{1+m n}$ for their values of $m$ and $n$ A1 - obtain $\tan A P B=\frac{4}{3}$ |

