

12	(a)	(i)	$\frac{d\theta}{dt} = -k$	B1 [1]	3.3	Allow $\frac{d\theta}{dt} = k$ or $\frac{d\theta}{dt} = -3.5$	Both sides of differential equation required
		(ii)	$\theta = -3.5t + c$ $\theta = 160 - 3.5t$	M1 A1 [2]	3.4 1.1	Obtain equation of the form $\theta = \pm 3.5t + c$, where c could already be numerical and possibly incorrect Obtain correct equation	Not dependent on correct differential equation in (i) Alt method For M1, integrate to get $\theta = kt + c$, then use (0, 160) and (10, 125) to attempt c and hence k

Question			Answer	Marks	AO	Guidance
		(iii)	The model would predict that the temperature would fall below room temperature, and eventually below freezing point	B1 [1]	3.5b	Any sensible comment Cooling rate unlikely to be linear Identify that limit (ie room temperature) will be reached

	(b)	(i)	$\frac{d\theta}{dt} = -k(\theta - 20)$	B1 [1]	3.3	Allow $\frac{d\theta}{dt} = k(\theta - 20)$ Both sides of differential equation required ISW if $k = -3.5$ used once correct equation seen (but B0 if only ever seen with -3.5)
		(ii)	$\int \frac{1}{\theta - 20} d\theta = \int -k dt$	M1	3.1a	Separate variables (or invert each side) and attempt integration Allow M1 for integration of a differential equation not of this form eg $\frac{d\theta}{dt} = \frac{-k}{(\theta - 20)}$, as long as t and/or θ are involved – must be attempt at correct rearrangement of their diff eqn

Question		Answer	Marks	AO	Guidance	
		$\ln \theta - 20 = -kt + c$ $\ln 140 = c$ $\ln 105 = -10k + \ln 140$ $k = -0.1 \ln 0.75$ $\ln \theta - 20 = (0.1 \ln 0.75)t + \ln 140$ $\theta - 20 = e^{(0.1 \ln 0.75)t + \ln 140} = 140e^{(0.1 \ln 0.75)t}$ $\theta = 20 + 140e^{(0.1 \ln 0.75)t}$	A1 M1 M1 M1 A1 [6]	1.1 3.4 1.1a 1.1 1.1	Obtain correct integral Use $t = 0, \theta = 160$ in an equation involving both k and c Use $t = 10, \theta = 125$ in an equation involving both k and c (c possibly now numerical) Attempt to make θ the subject Obtain correct equation Allow -0.0288 (or better) for $0.1 \ln 0.75$ and/or 4.94 (or better) for $\ln 140$	Or $\ln \theta - 20 = kt + c$ Condone brackets not modulus Equation must be from integration attempt, but could follow M0 As far as numerical c or k Using both pairs of values as limits in a definite integral is M2 As far as numerical c and k As far as correctly removing logs Equation must now be of the correct form ie $\ln a\theta + b = ct + d$ Could still be in terms of c and k to give eg $\theta = Ae^{kt} + 20$ Allow $\theta = 20 + e^{(0.1 \ln 0.75)t + \ln 140}$ Could see $\theta = 140(0.75)^{0.1t} + 20$
	(c)	$25 = 160 - 3.5t \Rightarrow t = 38.6$ mins $\ln 5 = (0.1 \ln 0.75)t + \ln 140 \Rightarrow t = 115.8$ mins 77 minutes	M1 A1 [2]	3.4 3.4	Use $\theta = 25$ in both of their equations to find values for t Obtain 77 minutes As far as two numerical values for t Accept any answer rounding to 77, with no errors seen	