

9		$dx = 2\cos\theta d\theta$ $\int \sqrt{4-x^2} dx = \int \sqrt{4-4\sin^2\theta} \cdot 2\cos\theta d\theta$ $= \int \sqrt{4\cos^2\theta} \cdot 2\cos\theta d\theta$ $= \int 4\cos^2\theta d\theta$ $= \int (2\cos 2\theta + 2) d\theta$ $= \sin 2\theta + 2\theta$ $\left[\sin 2\theta + 2\theta \right]_{\frac{1}{6}\pi}^{\frac{1}{3}\pi} = \left(\sin \frac{2}{3}\pi + \frac{2}{3}\pi \right) - \left(\sin \frac{2}{6}\pi + \frac{2}{6}\pi \right)$ $= \left(\frac{1}{2}\sqrt{3} + \frac{2}{3}\pi \right) - \left(\frac{1}{2}\sqrt{3} + \frac{1}{3}\pi \right)$ $= \frac{1}{3}\pi \quad \mathbf{A.G.}$	<p>M1 M1</p> <p>A1</p> <p>M1</p> <p>A1FT M1</p> <p>A1</p> <p>[7]</p>	<p>1.1a 3.1a</p> <p>1.1</p> <p>2.1</p> <p>1.1 2.1</p> <p>2.1</p>	<p>Attempt to link dx and dθ</p> <p>Attempt to write integrand in terms of θ</p> <p>Obtain correct integrand in terms of cosθ only</p> <p>Attempt use of double angle formula</p> <p>Integrate to obtain sin2θ + 2θ</p> <p>Attempt use of limits</p> <p>Obtain given answer of $\frac{1}{3}\pi$</p>	<p>Allow sign error only</p> <p>Must substitute for both function and dx</p> <p>Can follow M0 but do not allow just dx = dθ</p> <p>Condone no dθ, as long as previously seen</p> <p>Using cos2θ = ± 2cos²θ ± 1</p> <p>Integrand must be of form k cos²θ, which must have come from correct method with coefficient errors only</p> <p>FT on a cos2θ + b only</p> <p>Must be correct limits (either x or θ, as long as consistent with their integral), correct order and subtraction</p> <p>Allow M1 for use of limits in any integration attempt in terms of θ</p> <p>Allow M1 for either expressions that still involve sin, or exact equivalents</p> <p>M0 for decimal values, even if then stated to be the same as $\frac{1}{3}\pi$</p> <p>Condone eg $\frac{1}{2}\sqrt{3}$ from sin120°, but M0 if degrees used in linear term</p> <p>Must see both surd values, or an explanation as to why $\sin \frac{2}{3}\pi = \sin \frac{2}{6}\pi$</p>
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