

7 (a) Use the result $\cos(A + B) = \cos A \cos B - \sin A \sin B$ to show that

$$\cos(A - B) = \cos A \cos B + \sin A \sin B. \quad [2]$$

The function $f(\theta)$ is defined as $\cos(\theta + 30^\circ)\cos(\theta - 30^\circ)$, where θ is in degrees.

(b) Show that $f(\theta) = \cos^2\theta - \frac{1}{4}$. [3]

(c) (i) Determine the following.

- The **maximum** value of $f(\theta)$
- The smallest **positive** value of θ for which this maximum value occurs [2]

(ii) Determine the following.

- The **minimum** value of $f(\theta)$
- The smallest **positive** value of θ for which this minimum value occurs [2]