

5	(a)	$x^2 + y^2 = 4$ <p>When $x = 1$</p> $1 + y^2 = 4 \Rightarrow y = \sqrt{3}$ $y = \frac{1}{\sqrt{3}}(4 - 1) \Rightarrow y = \sqrt{3}$	B1	1.1	soi	
			E1	2.1	AG Check that Q lies on the circle	OR
			E1	2.1	AG Check that Q lies on the parabola	B1 $x^2 + (\sqrt{3})^2 = 4 \Rightarrow x = 1$
			[3]			B1 $\sqrt{3} = \frac{1}{\sqrt{3}}(4 - x^2) \Rightarrow x = 1$

Question		Answer	Marks	AO	Guidance	
5	(b)	$\frac{1}{\sqrt{3}} \int_{-1}^1 (4-x^2) dx$	M1	3.1a	Attempt correct integral and limits; may be implied by answer 4.23(39...)	OR M1 $\frac{1}{\sqrt{3}} \int_0^1 (4-x^2) dx =$ 2.1169...
		$= \frac{22\sqrt{3}}{9}$	A1	1.1	BC	A1 $= \frac{11\sqrt{3}}{9}$
		Let N be the point $(1, 0)$	B1	2.1		OR
		Area $OQN = \frac{\sqrt{3}}{2}$ oe or 0.866 (3 s.f.)				B1 semi-circle: $y = \sqrt{4-x^2}$
		$QON = \tan^{-1} \sqrt{3}$	M1	3.1a	Or $\sin^{-1}\left(\frac{\sqrt{3}}{2}\right)$ or $\cos^{-1}\left(\frac{1}{2}\right)$ or $\frac{1}{3}\pi$ or 60°	M1 attempt $\int_{-1}^1 \sqrt{4-x^2} dx$ by substitution, e.g. $x = 2\sin u$
		$POQ = \frac{1}{3}\pi$ or 60°	A1	1.1	M1A1 may be implied by seeing next line	M1 Use trigonometric identity e.g. $\int_{-\frac{1}{6}\pi}^{\frac{1}{6}\pi} 4\cos^2 u du = \int_{-\frac{1}{6}\pi}^{\frac{1}{6}\pi} a \cos 2u + b du$
		Area sector $POQ = \frac{1}{2} \times 2^2 \times \frac{1}{3}\pi$ oe $(= \frac{2}{3}\pi$ oe or 2.09 (3 s.f.))	M1	1.1	FT their angle POQ	A1 $\frac{2}{3}\pi + \sqrt{3}$
Shaded area $= \frac{22\sqrt{3}}{9} - 2 \times \frac{\sqrt{3}}{2} - \frac{2}{3}\pi$ oe	M1	3.2a	Correct combination of their areas	M1 Shaded area $= \frac{22\sqrt{3}}{9} - \frac{2}{3}\pi - \sqrt{3}$ oe		
$= \frac{13\sqrt{3}}{9} - \frac{2}{3}\pi$ oe	A1	1.1		A1 $= \frac{13\sqrt{3}}{9} - \frac{2}{3}\pi$ oe		
			[8]			