

8	(a)	<p><u>Summary scheme</u> Attempt separate variables using $(100 - P)$ Correct integral, but allowing $100 - P$ or $(P - 100)$ or $(100 - P)$ Attempt $t = 0, P = 2000$ to find c or A or $e^{\pm c}$</p>	<p>M1 A1 M1</p>	<p>3.1a 1.1 3.4</p>	<p>Allow without $+ c$ dep M1</p>
		<p>$c = -\ln 1900$ or $A = 1900$ or $e^{\pm c} = 1900$ OR Allow $c = \ln 1900$ or $-\ln(-1900)$ or A or $e^{\pm c} = -1900$ or $-\frac{1}{1900}$</p>	<p>A1</p>	<p>3.4</p>	<p>dep M1M1</p>
		<p>Attempt make P the subject Correct use of mod & change to $P - 100$ $P = 1900e^{-t} + 100$</p>	<p>M1 M1 A1</p>	<p>3.4 2.1 1.1</p>	<p>dep M1M1A1 dep M1A1M1A1M1M1 ie dep all correct working seen</p>
		<p>Examples of correct methods</p> $\frac{dP}{100-P} = dt$ $-\ln 100 - P = t + c \quad \text{or} \quad 100 - P = Ae^{-t}$ <p>Substitute $t = 0, P = 2000$</p> $\Rightarrow c = -\ln 1900 \quad \text{or} \quad A = 1900$ $\ln \frac{ 100-P }{1900} = -t \quad \text{or} \quad 100 - P = 1900e^{-t}$ $\frac{P-100}{1900} = e^{-t}$ $P = 1900e^{-t} + 100$	<p>M1 A1 M1 A1 M1 A1 A1</p>		

Question			Answer	Mark	AO	Guidance
8	(a)	ctd	$\frac{dP}{P-100} = -dt$ $\ln(P-100) = -t + c$ or $P-100 = Ae^{-t}$ Substitute $t = 0, P = 2000$ $\Rightarrow c = \ln 1900$ correct or $A = 1900$ $\ln(P-100) = -t + \ln 1900$ or $P-100 = 1900e^{-t}$ $\frac{P-100}{1900} = e^{-t}$ $P = 1900e^{-t} + 100$	M1 M1 A1 M1 A1		
			<p>Example of incorrect methods</p> $\frac{dP}{100-P} = dt$ $-\ln(100-P) = t + c$ or $100-P = Ae^{-t}$ $100-P = e^{-t-c}$ Substitute $t = 0, P = 2000$ $\Rightarrow e^{-c} = -1900$ or $A = -1900$ $100-P = -1900e^{-t}$ oe No change to $P-100$ $P = 1900e^{-t} + 100$	M1 A1 M1 A1 M0 M1 A0		(Correct answer but incorrectly obtained, not using modulus
			$\frac{dP}{100-P} = dt$ $\ln(100-P) = t + c$ Substitute $t = 0, P = 2000$ $\ln(-1900) = c$ $\ln(100-P) = t + \ln(-1900)$ $100-P = -1900e^t$ No change to $P-100$ $P = 100 + 1900e^t$	M1 A0 M1 A1 M0 M1 A0		

Question		Answer	Mark	AO	Guidance	
8	(b)	(Starts at 2000)	Decreases	B1f	3.4	B1 for correct process or ft (a) dep (a) includes exponential
			Approaches 100	B1f	3.4	B1 for correct limit or ft (a) dep (a) includes exponential
				[2]		