				NB Other correct methods may be seen
$(3m+0)^2 = 9m^2$		B1	3.1a	$9m^2$ alone, not as part of longer expression
$(3m+1)^2 = 9m^2 + 6m + 1$	$(3m+2)^2 = 9m^2 + 12m + 4$	M1	1.1	At least one of these expansions attempted using $r = 1$ or 2. Must include three (or four) terms, Allow one error
$= 3(3m^2 + 2m) + 1$ $= 3(3m^2 + 4m + 1) + 1$ or $3(3m^2 + 4m) + 4$ None of these is of the form $3n + 2$ Allow "\neq 3n + 2"		A1 A1	2.1 3.2a	At least one of these seen explicitly Must see the statement oe. Can be seen once at end or with each separate case Dep complete method, with all three cases seen
$(3m + r)^2$ = 3(3m <sup>2</sup> + 2mr) + r <sup>2</sup> = 3n + r <sup>2</sup> But r <sup>2</sup> = 0, 1 or 4	$(=9m^2+6mr+r^2)$	M1 A1 B1		Attempted. Must include 3 (or 4) terms, Allow one error Explicit
Alternative method 2  Let $(3m + r)^2 = 3n + 2$ $3(3m^2 + 2mr - n) = 2 - r^2$ Hence $2 - r^2$ is divisible by 3  But $2 - 0^2 = 2$ , $2 - 1^2 = 1$ , $2 - 2^2 = -2$ None of these is divisible by 3		M1 A1 B1		Must see the statement oe Dep complete method
	$(3m + 1)^2$ = $9m^2 + 6m + 1$ = $3(3m^2 + 2m) + 1$ None of these is of the Allow " $\neq 3n + 2$ " <b>Alternative method</b> 1 $(3m + r)^2$ = $3(3m^2 + 2mr) + r^2$ = $3n + r^2$ But $r^2 = 0$ , 1 or 4 Hence not in the form <b>Alternative method</b> 2 Let $(3m + r)^2 = 3n + 2$ $3(3m^2 + 2mr - n) = 2$ Hence $2 - r^2$ is divisite But $2 - 0^2 = 2$ , $2 - 1^2$	$(3m+1)^{2} = 9m^{2} + 6m + 1$ $= 3(3m^{2} + 2m) + 1$ $= 3(3m^{2} + 4m + 1) + 1$ or $3(3m^{2} + 4m) + 4$ None of these is of the form $3n + 2$ Allow "\neq 3n + 2"  Alternative method 1 $(3m+r)^{2} = 3(3m^{2} + 2mr) + r^{2}$ $= 3n + r^{2}$ But $r^{2} = 0$ , 1 or 4 Hence not in the form $3n + 2$ for any $r$ Alternative method 2 Let $(3m+r)^{2} = 3n + 2$ $3(3m^{2} + 2mr - n) = 2 - r^{2}$ Hence $2 - r^{2}$ is divisible by 3 But $2 - 0^{2} = 2$ , $2 - 1^{2} = 1$ , $2 - 2^{2} = -2$	$(3m+1)^{2} = 9m^{2} + 6m + 1$ $= 3(3m^{2} + 2m) + 1$ $= 3(3m^{2} + 4m + 1) + 1$ or $3(3m^{2} + 4m) + 4$ None of these is of the form $3n + 2$ Allow " $\neq 3n + 2$ "  [4]  Alternative method 1 $(3m + r)^{2} = 3(3m^{2} + 2mr) + r^{2}$ $= 3(3m^{2} + 2mr) + r^{2}$ $= 3n + r^{2}$ But $r^{2} = 0$ , 1 or 4 Hence not in the form $3n + 2$ for any $r$ Alternative method 2 Let $(3m + r)^{2} = 3n + 2$ $3(3m^{2} + 2mr - n) = 2 - r^{2}$ Hence $2 - r^{2}$ is divisible by 3 But $2 - 0^{2} = 2$ , $2 - 1^{2} = 1$ , $2 - 2^{2} = -2$	$(3m+1)^{2} = 9m^{2} + 6m + 1$ $= 3(3m^{2} + 2m) + 1$ $= 3(3m^{2} + 4m + 1) + 1$ or $3(3m^{2} + 4m) + 4$ A1

Question		n	Answer		AO	Guidance
7	(a)	ctd	Alternative method 3 $(3m)^2 = (9m^2 - 2) + 2$ $(3m+1)^2 = (9m^2 + 6m - 1) + 2$ $(3m+2)^2 = (9m^2 + 12m + 2) + 2$ $(9m^2 - 2) = 3(3m^2) - 2$ $(9m^2 + 6m - 1) = 3(3m^2 + 2m) - 1$ $(9m^2 + 12m + 2) = 3(3m^2 + 4m) + 2$ Hence none is divisible by 3	B1 M1 A1		Allow one arithmetical error Both correct or $3(3m^2 - \frac{2}{3}) + 2$ or $3(3m^2 + 2m - \frac{1}{3}) + 2$ or $3(3m^2 + 4m + \frac{2}{3}) + 2$ None of the brackets is an integer
7	(b)		Either imply three digits all of the same type or imply three digits all of different types $P(0, 0, 0) \text{ or } P(1, 1, 1) \text{ or } P(2, 2, 2): \qquad \left(\frac{1}{3}\right)^3$ $P(0, 1, 2): \qquad \qquad \left(\frac{1}{3}\right)^3 \times 6$ or $1 \times \frac{2}{3} \times \frac{1}{3}$ oe	M1* M1 dep M1 dep		Could be numerical or algebraic or in words If listed, must be clear which ones are selected  M1 for $\left(\frac{1}{3}\right)^3$ associated with at least one of these  M1 for $\left(\frac{1}{3}\right)^3 \times k$ where $k = 4$ , 5 or 6, associated with $(0, 1, 2)$
			Alternative method for $2^{nd}$ & $3^{rd}$ M1M1 No. of cases = $3^3 = 27$ No. divisible by $3 = (3 + 6 =) 9$	M1 M1		Allow 7 or 8
			$\frac{9}{27}$ or $\frac{1}{3}$ or 0.333 (3 sf)	A1	1.1	Correct answer with no working: M0M0M0A0

