

7 It is given that any integer can be expressed in the form $3m+r$, where m is an integer and r is 0, 1 or 2.

Use this fact to answer the following.

- (a) By considering the different values of r , prove that the square of any integer **cannot** be expressed in the form $3n+2$, where n is an integer. [4]
- (b) Three integers are chosen at random from the integers 1 to 99 inclusive. The three integers are not necessarily different.

By considering the different values of r , determine the probability that the sum of these three integers is divisible by 3. [4]