

Question		Answer	Mark	AO	Guidance
4	(a)	$\frac{dy}{dx} = 2x.$ <p>Gradient of tangent at (1, 1) is 2 Gradient of normal at (1, 1) = $-\frac{1}{2}$</p> <p>Equation of normal is $y - 1 = -\frac{1}{2}(x - 1)$</p> <p>At B: $x^2 = -\frac{1}{2}x + \frac{3}{2}$</p> $2x^2 + x - 3 = 0$ <p>B is $(-\frac{3}{2}, \frac{9}{4})$</p>	M1 A1 M1* M1 dep* A1 A1 [6]	3.1a 1.1 1.1 3.1a 1.1 1.1	<p>For correct gradient of either tangent or normal</p> <p>Using their gradient of normal and (1,1) to form an equation or $y = -\frac{1}{2}x + \frac{3}{2}$ (must find a value for c for this mark to be awarded) FT their gradient of normal (not = 2)</p> <p>Substituting $y = x^2$ and attempting to solve (may see quadratic in x or y)</p> <p>Correct quadratic in x or y, in any form or $4y^2 - 13y + 9 = 0$</p> <p>Allow (-1.5,2.25). Accept $x=...$, $y=...$ but must see both.</p>
4	(b)	$AB^2 = \left(1 - \left(-\frac{3}{2}\right)\right)^2 + \left(1 - \frac{9}{4}\right)^2 \quad \left(= \frac{125}{16}\right)$ $OB^2 = \left(\frac{3}{2}\right)^2 + \left(\frac{9}{4}\right)^2 \quad \left(= \frac{117}{16}\right)$ $OA^2 = 2$ $\cos \alpha = \frac{\frac{117}{16} + 2 - \frac{125}{16}}{2 \times \sqrt{\frac{117}{16}} \times \sqrt{2}}$ $\cos \alpha = \frac{1}{\sqrt{26}} \quad \text{OR} \quad \tan \alpha = \frac{\sqrt{26}-1}{1}$ $\tan \alpha = 5$	M1 M1 dep A1	2.1 1.1 1.1	<p>or $AB = \frac{5\sqrt{5}}{4}$</p> <p>or $OB = \frac{3\sqrt{13}}{4}$</p> <p>or $OA = \sqrt{2}$</p> <p>Attempt to find all three, squared or not (may see on diagram)</p> <p>Correct use of cos rule in any form, FT their AB, OB & OA</p> <p>Must be exact and come from exact working for cos α. Must see an exact intermediate step – either $\frac{1}{\sqrt{26}}$ or $\frac{\sqrt{26}-1}{1}$.</p> <p>Decimals used throughout can achieve max [2/3] M1M1A0</p> <p>Do not penalise candidates who write down $\alpha = 78.69\dots^\circ$ but the final answer must come from exact working (not BC).</p>

<p>Alternative method (1)</p> $\tan \beta = \frac{9}{4} \div \frac{3}{2} = \frac{3}{2}, \tan \gamma = 1$ $\tan \alpha = -\tan(\beta + \gamma) = -\frac{\frac{3}{2} + 1}{1 - \frac{3}{2} \times 1}$ $= 5$	<p>M1</p> <p>M1 dep</p> <p>A1</p>	<p>Attempt to find $\tan \beta$ & $\tan \gamma$ β and γ are the angles made by OB and OA respectively with the horizontal (Alternatively with angles to the vertical, $\tan \beta = \frac{2}{3}$) Correct use of $\tan(180 - \theta) = -\tan \theta$ and $\tan(A + B)$ formula using their $\tan \beta$ & $\tan \gamma$ (or, with angles to the vertical, $\tan \alpha = \frac{1 + \frac{2}{3}}{1 - \frac{2}{3} \times 1}$) Must be exact and come from exact working. Do not penalise candidates who write down $\alpha = 78.69\dots^\circ$ but the final answer must come from exact working (not BC).</p>
<p>Alternative method (2)</p> $\tan BOx = \frac{9}{4} \div (-\frac{3}{2}) = -\frac{3}{2}, \tan AOx = 1$ $\tan(BOx - AOx)$ $= \frac{-\frac{3}{2} - 1}{1 + (-\frac{3}{2}) \times 1}$ $= 5$	<p>M1</p> <p>M1 dep</p> <p>A1</p>	<p>Attempt find $\tan BOx$ & $\tan AOx$ and use $\tan(\theta - \phi)$ formula Correct use of $\tan(\theta - \phi)$ using their $\tan BOx$ & $\tan AOx$ Must be exact and come from exact working.</p>
<p>Alternative method (3)</p> $\overrightarrow{OB} \cdot \overrightarrow{OA} = -\frac{3}{2} + \frac{9}{4} = \sqrt{2} \times \frac{3\sqrt{13}}{4} \cos \alpha$ $\cos \alpha = \frac{\frac{3}{4}}{\sqrt{2 \times \frac{117}{16}}}$ $\cos \alpha = \frac{1}{\sqrt{26}} \text{ OR } \tan \alpha = \frac{\sqrt{26-1}}{1}$ $\tan \alpha = 5$	<p>M1</p> <p>M1 dep</p> <p>A1</p> <p>[3]</p>	<p>Attempt $\overrightarrow{OB} \cdot \overrightarrow{OA}$ Correct dot product with exact values Must be exact and come from exact working for $\cos \alpha$. Must see an exact intermediate step – either $\frac{1}{\sqrt{26}}$ or $\frac{\sqrt{26-1}}{1}$.</p>