

Question	Answer	Mark	AO	Guidance
6	<p data-bbox="321 56 383 88">DR</p> $2x^2 - 6x + a = 0$ $\text{At } A: x = \frac{6 + \sqrt{36 - 8a}}{4} = \frac{3 - \sqrt{9 - 2a}}{2}$ $\text{At } B: x = \frac{3 + \sqrt{9 - 2a}}{2}$ $\text{At } M: x = \frac{3}{2}$ $CM^2 = \left(3 - \frac{3}{2}\right)^2 + \left(\frac{3}{2}\right)^2 \quad (= \frac{9}{2})$ $BA^2 = (\sqrt{9 - 2a})^2 + (\sqrt{9 - 2a})^2$ $\quad (= 2(\sqrt{9 - 2a})^2)$ $\text{Area} = \frac{1}{2} \times CM \times BA$ $\frac{1}{2} \times \sqrt{2}\sqrt{9 - 2a} \times \frac{3}{\sqrt{2}} \quad (= 3\sqrt{\frac{9 - 2a}{4}}) \text{ AG}$	<p data-bbox="942 207 1004 238">M1</p> <p data-bbox="942 404 1004 435">A1</p> <p data-bbox="942 523 1004 554">A1</p> <p data-bbox="942 595 1004 626">M1</p> <p data-bbox="942 694 1004 725">M1</p> <p data-bbox="942 859 1004 890">M1</p> <p data-bbox="942 932 1004 963">A1</p>	<p data-bbox="1046 207 1108 238">3.1a</p> <p data-bbox="1046 404 1108 435">2.2a</p> <p data-bbox="1046 523 1108 554">1.1</p> <p data-bbox="1046 595 1108 626">2.1</p> <p data-bbox="1046 694 1108 725">1.1</p> <p data-bbox="1046 859 1108 890">1.1</p> <p data-bbox="1046 932 1108 963">1.1</p>	<p data-bbox="1129 56 2040 165">In this question, if candidates attempt more than one method, review all their working to identify which is their ‘final’ or ‘substantially most complete’ answer, then apply one scheme only. Candidates cannot gain marks from more than one scheme.</p> <p data-bbox="1129 170 2040 279">Substitute $y = x$ into equation of circle (need not be simplified – may see this quadratic in y)</p> <p data-bbox="1129 404 2040 476">A1 for <u>either</u> correct (condone if not specifically identified as A or B – may see $y =$ these values)</p> <p data-bbox="1129 523 2040 631">A1 1.1</p> <p data-bbox="1129 595 2040 694">Attempt CM using their values (method must be correct) May see $CM = \frac{3\sqrt{2}}{2}$</p> <p data-bbox="1129 694 2040 797">Attempt BA using their values (method must be correct) May see just $\sqrt{2(9 - 2a)}$ oe, e.g. $\sqrt{18 - 4a}$</p> <p data-bbox="1129 797 2040 859">Alternative: $AM = \sqrt{\frac{9}{2} - a}$ (and then $Area = 2 \times \frac{1}{2} \times CM \times AM$)</p> <p data-bbox="1129 859 2040 890">Attempt at area, in terms of a</p> <p data-bbox="1129 932 2040 963">Must see correct expression before answer</p>

Alternative Method

DR $(x - 3)^2 + y^2 = 9 - a$

C is $(3, 0)$; radius = $\sqrt{9 - a}$

$CM = (3\cos 45^\circ) = \frac{3}{\sqrt{2}}$

$AM^2 = (9 - a) - \left(\frac{3}{\sqrt{2}}\right)^2 \quad (= \frac{9}{2} - a)$

Area = $AM \times CM$ or $\frac{1}{2}AB \times CM$

$= \sqrt{\frac{9}{2} - a} \times \frac{3}{\sqrt{2}}$ oe

$= \sqrt{\frac{9 - 2a}{2}} \times \frac{3}{\sqrt{2}} \quad (= 3\sqrt{\frac{9 - 2a}{4}} \quad \mathbf{AG})$

M1Attempt complete the square for x **A1**

Both soi

B1Possibly coming from $\frac{|3-0|}{\sqrt{1^2+1^2}}$ **M1**Their radius² (in terms of a) – their CM^2 **M1**Attempted in terms of a **A1FT**FT their AM or AB (in terms of a), and their CM **A1**

Must see one correct intermediate step

Alternative method for last three marks

Area = $\frac{1}{2}AB \times r \times \sin BAC$

$= \sqrt{\frac{9}{2} - a} \times \sqrt{9 - a} \times \left(\frac{3}{\sqrt{2}} \div \sqrt{9 - a}\right)$

$= \sqrt{\frac{9 - 2a}{2}} \times \frac{3}{\sqrt{2}} \quad (= 3\sqrt{\frac{9 - 2a}{4}} \quad \mathbf{AG})$

M1Attempted in terms of a **A1FT**FT their r and AM or AB (in terms of a), and their CM **A1**

Must see one correct intermediate step

Alternative method for last three marks

Area = $\frac{1}{2}r \times r \times \sin BCA$

$= \sqrt{9 - a} \times \sqrt{9 - a} \times 2 \left(\sqrt{\frac{9}{2} - a} \div \sqrt{9 - a} \right) \left(\frac{3}{\sqrt{2}} \div \sqrt{9 - a} \right)$

A1FTFT their r and AM or AB (in terms of a), and their CM (using double angle formula for $\sin BCA$)

$= \sqrt{\frac{9 - 2a}{2}} \times \frac{3}{\sqrt{2}} \quad (= 3\sqrt{\frac{9 - 2a}{4}}) \quad \mathbf{AG}$

A1

Must see one correct intermediate step

[7]

6	(b)	(i)	$(3\sqrt{\frac{9-2a}{4}} = 0 \Rightarrow) a = \frac{9}{2}$	B1	2.2a	oe
				[1]		
6	(b)	(ii)	$y = x$ is a tangent to the circle or A and B are coincident oe	B1	3.2a	Must see this geometrical answer (accept e.g. the line touches the circle) Accept a diagram that clearly shows the line is a tangent
				[1]		
6	(c)		Line $y = x$ does not meet circle	B1	3.2a	Must see this geometrical answer (condone BOD for 'the line does not touch the circle') Accept a diagram that clearly shows the line does not meet the circle
				[1]		