

10 In this question the unit vectors \mathbf{i} and \mathbf{j} are in the directions east and north respectively.

A particle R of mass 2 kg is moving on a smooth horizontal surface under the action of a single horizontal force $\mathbf{F}\text{ N}$. At time t seconds, the velocity $\mathbf{v}\text{ ms}^{-1}$ of R , relative to a fixed origin O , is given by $\mathbf{v} = (pt^2 - 3t)\mathbf{i} + (8t + q)\mathbf{j}$, where p and q are constants and $p < 0$.

(a) Given that when $t = 0.5$ the magnitude of \mathbf{F} is 20 , find the value of p . **[6]**

When $t = 0$, R is at the point with position vector $(2\mathbf{i} - 3\mathbf{j})\text{ m}$.

(b) Find, in terms of q , an expression for the displacement vector of R at time t . **[4]**

When $t = 1$, R is at a point on the line L , where L passes through O and the point with position vector $2\mathbf{i} - 8\mathbf{j}$.

(c) Find the value of q . **[3]**