

12	(a)		$\mathbf{v} = (1 - 2t)\mathbf{i} + (2t^2 + t - 13)\mathbf{j}$ If P is stationary, then $1 - 2t = 0$ and $2t^2 + t - 13 = 0$ $\mathbf{i}: 1 - 2t = 0 \Rightarrow t = \frac{1}{2}$ $\mathbf{j}: 2t^2 + t - 13 = 0 \Rightarrow t = 2.3117..., -2.8117...$ No value of t is common to both components, so P is never stationary	M1 A1 [2]	3.1b 2.2a	Considers either the i or j component equal to zero or forms a five-term quartic equation for $ \mathbf{v} ^2 = 0$ (oe) $(4t^4 + 4t^3 - 47t^2 - 30t + 170 = 0)$ BC – need not see the negative value of t or for substituting $t = 0.5$ into quadratic expression for j and showing this gives a non-zero answer (oe) with correct working and conclusion	A1 for the correct quartic equation with roots stated as $2.3 \pm 0.35\mathbf{i}$, $-2.8 \pm 0.65\mathbf{i}$ + correct conclusion
12	(b)		$\Rightarrow \mathbf{a} = -2\mathbf{i} + (4t + 1)\mathbf{j} \text{ (m s}^{-2}\text{)}$	B1 [1]	1.1	Correct derivative – or as a column vector	Brackets must be around the $4t + 1$

12	(c)	$-2(2t^2 + t - 13) = 1(1 - 2t)$ $4t^2 - 25 = 0 \Rightarrow t = 2.5$ $\mathbf{F} = m\mathbf{a} \Rightarrow \mathbf{F} = 0.5\{-2\mathbf{i} + (4t + 1)\mathbf{j}\}$ $ \mathbf{F} = \sqrt{(-1)^2 + 5.5^2}$ $ \mathbf{F} = 5.59 \text{ (N)}$	M1* M1dep* M1* M1dep* A1 [5]	3.1b 1.1 3.4 1.1 1.1	Setting up a quadratic equation in t only – allow sign errors (including on the 1 and 2) and the 1 and –2 on the wrong side Solves their (two or three term) quadratic and selects their positive value of t Substitute their $\mathbf{a}$ into $\mathbf{F} = 0.5\mathbf{a}$ or their $\mathbf{a}$ into $\mathbf{F} = 0.5 \mathbf{a}$. If $\mathbf{F}$ not stated in terms of t then one component must be correct following through from their $\mathbf{a}$ (and possibly t) Dependent on previous M mark only awrt 5.59 (exact: $\frac{5\sqrt{5}}{2}$)	Or multiples of 1 and –2 Check unsupported solutions if incorrect quadratic equation Must use correct value of 0.5 for m but can be in terms of t From a value of $t > 0$ 5.590169...
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12	(d)	$\mathbf{s} = (t - t^2)\mathbf{i} + \left(\frac{2}{3}t^3 + \frac{1}{2}t^2 - 13t\right)\mathbf{j} (+\mathbf{c})$ $t = 1, \mathbf{s} = \frac{1}{6}\mathbf{j} \Rightarrow \mathbf{c} = (0\mathbf{i} +)12\mathbf{j}$ When $t = 1.5$, $\mathbf{s} = -\frac{3}{4}\mathbf{i} - \frac{33}{8}\mathbf{j}$ $\tan^{-1}\left(\frac{\pm 3/4}{\pm 33/8}\right) \text{ or } \tan^{-1}\left(\frac{\pm 33/8}{\pm 3/4}\right)$ $\text{Bearing} = 180 + \tan^{-1}\left(\frac{3/4}{33/8}\right) = 190^\circ$	M1* A1 M1dep* M1 A1 [5]	1.1 3.4 1.1 3.1b 3.2a	Integrates $\mathbf{v}$ wrt t – at least three terms correct Uses given conditions to find correct $\mathbf{c}$ – dependent on a completely correct integrated expression for $\mathbf{s}$ Substitute $t = 1.5$ into their $\mathbf{s}$ Attempt to find a relevant angle using the components of their $\mathbf{s}$ (allow use of sin/cos with the magnitude of $\mathbf{s}$) awrt 190 (or from $270 - \tan^{-1}\left(\frac{33/8}{3/4}\right)$)	Allow without $+\mathbf{c}$ www Dependent on both previous M marks. Written in terms of arctan is sufficient 190.3048465...
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