

Question		Answer	Marks	AO	Guidance	
12	(a)		B1	1.1	Quadratic curve (positive quadratic) passing through the origin and appearing in both quadrants with a minimum turning point in the fourth quadrant	No scaling on axes required for the first two <b>B</b> marks (so <b>ignore any scaling for the first two marks</b> )
			B1	1.1	Inverse proportional (to $t^2$ ) curve (so correct curvature), should not touch the horizontal axis	Condone if it appears to be approaching a horizontal asymptote (other than the $t$ -axis) for this mark but gradient must not be positive
			B1	1.1	Completely correct graph with both curves meeting at 6 <b>with values of 3 and 6 on <math>t</math> axis</b> (or clearly stated in their working in part (a) only) – this mark is dependent on the previous 2 <b>B</b> marks	Allow only the $t$ -axis as a horizontal asymptote  <b>Value of 9 not required on <math>t</math> axis, neither is <math>\frac{3}{2}k</math> on the <math>v</math>-axis</b>
			[3]			
12	(b)	1.5 (s) only	B1	1.1	From symmetry or solving $\frac{1}{12}k(2t-3)=0$ www	Any other answer(s) is <b>B0</b>
			[1]			

Question	Answer	Marks	AO	Guidance
<p>12</p> <p>(c)</p>	<p><b>DR</b></p> $[k] \frac{1}{12} \int (t^2 - 3t) dt = \frac{1}{12} \left( \frac{t^3}{3} - \frac{3}{2} t^2 \right) [k]$ <p>For <b>both</b> <math>[k] \frac{1}{12} \int_0^3 (t^2 - 3t) dt = -\frac{3}{8}[k]</math> <b>or</b> <math>+\frac{3}{8}[k]</math>  <b>and</b> <math>[k] \frac{1}{12} \int_3^6 (t^2 - 3t) dt = \frac{15}{8}[k]</math> <b>(but allow correct un-simplified expressions – SEE APPENDIX)</b></p> $[k] \int \frac{54}{t^2} dt = -\frac{54}{t} [k]$ $[k] \int_6^9 \frac{54}{t^2} dt = 3[k]$ <p><b>(allow correct un-simplified – SEE APPENDIX)</b></p> $\frac{3}{8}k + \frac{15}{8}k + 3k = 84 \quad \text{or} \quad \frac{18}{8}k + 3k = 84$ <p><math>k = 16</math></p>	<p><b>M1*</b></p> <p><b>B1</b></p> <p><b>M1*</b></p> <p><b>B1</b></p> <p><b>M1dep*</b></p> <p><b>B1</b></p> <p><b>[6]</b></p>	<p><b>2.1</b></p> <p><b>1.1</b></p> <p><b>1.1</b></p> <p><b>1.1</b></p> <p><b>3.4</b></p> <p><b>2.2a</b></p>	<p>Attempt to integrate – <b>both terms with power increased by 1 with one term correct</b></p> <p>Ignore <math>+c</math> omission for <b>M</b> marks</p> <p>www</p> <p>Condone <math>[k] \frac{1}{12} \int_0^3 (t^2 - 3t) dt = +\frac{3}{8}[k]</math></p> <p>Award <b>B1</b> for</p> $[k] \frac{1}{12} \int_0^6 (t^2 - 3t) dt = \frac{18}{8}[k] \text{ but}$ <p><b>B0</b> for <math>[k] \frac{1}{12} \int_0^6 (t^2 - 3t) dt = \frac{12}{8}[k]</math></p> <p>Attempt to integrate – answer of the form <math>ct^{-1}</math> with <math>c \neq 1, 54k, 54</math></p> <p>www</p> <p>The correct value does not imply the <b>M</b> mark as <b>DR</b></p> <p>Forming a linear equation in <math>k</math> with the correct number of relevant terms (e.g. must have taken the modulus of their integral from 0 to 3)</p> <p>www</p> <p>The correct value does not imply the <b>M</b> mark as <b>DR</b></p> $\frac{1}{12}k \int_0^6 (t^2 - 3t) dt = \frac{12}{8}k,$ <p>or any working that suggests the modulus was not taken between 0 and 3 is <b>M0</b></p>

**Additional Guidance for 12(c)**

The square brackets around the  $k$  in the main scheme means that this may be omitted as they could deal with this constant at the end when they form their equation with the 84 (as the  $k$  is a constant factor for both expressions for  $v$ )

The first **B** mark is for a correct expression/value **for both**  $I_1 = [k] \frac{1}{12} \int_0^3 (t^2 - 3t) dt$  **and**  $I_2 = [k] \frac{1}{12} \int_3^6 (t^2 - 3t) dt$  in any un-simplified form:

so for  $I_1$  any expression that is equivalent to  $\pm \frac{1}{12} \left( \frac{3^3}{3} - \frac{3(3)^2}{2} \right) [k]$  is fine (allow either positive or negative due to the fact that this area is below the  $t$ -axis) e.g.

$I_1 = \pm \frac{1}{12} \left( 9 - \frac{27}{2} \right) [k]$  or  $\pm \frac{9}{24} [k]$  etc. (ISW once a correct un-simplified form is seen)

For  $I_2$  any expression that is equivalent to  $\frac{1}{12} \left( \frac{6^3}{3} - \frac{3(6)^2}{2} \right) [k] - \frac{1}{12} \left( \frac{3^3}{3} - \frac{3(3)^2}{2} \right) [k]$  is fine e.g.  $\frac{1}{12} (72 - 54) [k] - \frac{1}{12} \left( 9 - \frac{27}{2} \right) [k]$  or  $\left( \frac{3}{2} + \frac{3}{8} \right) [k]$  etc.

If the candidate does not consider these two integrals separately and instead attempts to combine as a single integral (between 0 and 6) then they must consider it correctly (given the applied context) so e.g.

$I_{1,2} = [k] \frac{1}{12} \int_0^6 (t^2 - 3t) dt = -\frac{1}{12} \left( \frac{3^3}{3} - \frac{3(3)^2}{2} \right) [k] + \frac{1}{12} \left( \frac{6^3}{3} - \frac{3(6)^2}{2} \right) [k] - \frac{1}{12} \left( \frac{3^3}{3} - \frac{3(3)^2}{2} \right) [k]$  scores **B1** but  $+\frac{1}{12} \left( \frac{3^3}{3} - \frac{3(3)^2}{2} \right) [k] + \frac{1}{12} \left( \frac{6^3}{3} - \frac{3(6)^2}{2} \right) [k] - \frac{1}{12} \left( \frac{3^3}{3} - \frac{3(3)^2}{2} \right) [k]$  is **B0**

The second **B** mark is for a correct expression/value for  $I_3 = 54[k] \int_6^9 t^{-2} dt$  in any un-simplified form: e.g.  $I_3 = 54 \left( -\frac{1}{9} - \left( -\frac{1}{6} \right) \right) [k]$  or  $54 \left( -\frac{1}{9} + \frac{1}{6} \right) [k]$  etc. (ISW once a correct un-simplified form is seen)

The third **M** mark is for considering  $|I_1| + I_2 + I_3 = 84$  to form a linear equation in  $k$  (with the correct number of relevant terms) – this mark is dependent on the first two **M** marks and also they must have taken the modulus or equivalent for their integral between 0 and 3 for this mark e.g. they must have considered  $-[k] \frac{1}{12} \int_0^3 (t^2 - 3t) dt$  **or**  $[k] \frac{1}{12} \int_3^0 (t^2 - 3t) dt$  oe

As this question is detailed reasoning the stages as shown in the MS must all be done to award each corresponding mark. So, an answer of  $k = 16$  with no working scores **B1** only.