

| Question |      | Answer  | Marks  | AO   |                       | Guidance   |                                |
|----------|------|---|--|--|-----------------------|--|--------------------------------|
| 6        | (i)  | $\sin(2\theta + \frac{\pi}{4}) = 3 \cos(2\theta + \frac{\pi}{4})$<br>$\sin 2\theta \cos \frac{\pi}{4} + \sin \frac{\pi}{4} \cos 2\theta = 3 \cos 2\theta \cos \frac{\pi}{4} - 3 \sin 2\theta \sin \frac{\pi}{4}$<br>$4 \sin 2\theta = 2 \cos 2\theta$<br>$2 \frac{\sin 2\theta}{\cos 2\theta} = 1 \Rightarrow \tan 2\theta = \frac{1}{2}$ | <b>M1</b><br><b>A1</b><br><b>A1</b><br><b>[3]</b>                                | <b>1.1</b><br><b>1.1</b><br><b>2.2a</b>                              | E<br>E                | <p>Correct use of compound angle formulae at least once</p> <p>Not from incorrect working</p> <p><b>AG</b> – at least one step of intermediate working seen</p>  |                                |
|          |      | <b>ALT:</b> $\tan(2\theta + \frac{\pi}{4}) = 3$<br>$\frac{\tan 2\theta + 1}{1 - \tan 2\theta} = 3 \Rightarrow \tan 2\theta + 1 = 3(1 - \tan 2\theta)$<br>$\tan 2\theta = \frac{1}{2}$   | <b>B1</b><br><b>M1</b><br><b>A1</b>  |  |                       | <p>Correct use of compound angle formula for tan and removal of fraction</p>   |                                |
| 6        | (ii) | $\tan 2\theta = \frac{1}{2} \Rightarrow \frac{2 \tan \theta}{1 - \tan^2 \theta} = \frac{1}{2}$<br>$\tan^2 \theta + 4 \tan \theta - 1 = 0$<br>$\tan \theta = -2 \pm \sqrt{5}$<br>$-2 + \sqrt{5} > 0$ so $\tan \theta = -2 + \sqrt{5}$ gives acute angle<br>$\therefore \tan \theta = -2 - \sqrt{5}$  | <b>M1*</b><br><b>Dep*M1</b><br><b>A1</b><br><b>A1</b><br><b>A1</b><br><b>[5]</b> | <b>3.1a</b><br><b>1.1</b><br><b>1.1</b><br><b>2.3</b><br><b>2.2a</b> | E<br>E<br>C<br>A<br>A | <p>Double angle formula for <math>\tan 2\theta</math></p> <p>Rearranges correctly to form 3-term quadratic in tan</p> <p><b>BC</b> - One correct exact value</p> <p>Explicit rejection and reason for rejection</p> <p>This value only</p> | Allow one sign slip in formula |