

The diagram shows the part of the curve  $y = 3x \sin 2x$  for which  $0 \le x \le \frac{1}{2}\pi$ .

The maximum point on the curve is denoted by P.

- (a) Show that the x-coordinate of P satisfies the equation  $\tan 2x + 2x = 0$ . [3]
- (b) Use the Newton-Raphson method, with a suitable initial value, to find the x-coordinate of P, giving your answer correct to 4 decimal places. Show the result of each iteration. [4]
- The trapezium rule, with four strips of equal width, is used to find an approximation to  $\int_{1}^{\frac{1}{2}\pi} 3x \sin 2x \, \mathrm{d}x.$

Show that the result can be expressed as  $k\pi^2(\sqrt{2}+1)$ , where k is a rational number to be determined. [4]

- (i) Evaluate  $\int_0^{\frac{1}{2}\pi} 3x \sin 2x \, dx.$ 
  - (ii) Hence determine whether using the trapezium rule with four strips of equal width gives an under- or over-estimate for the area of the region enclosed by the curve  $y = 3x \sin 2x$ and the *x*-axis for  $0 \le x \le \frac{1}{2}\pi$ . [1]

[1]

(iii) Explain briefly why it is not easy to tell from the diagram alone whether the trapezium rule with four strips of equal width gives an under- or over-estimate for the area of the region in this case. [1]