

5	(a)	$\frac{dy}{dt} = 3t^2 e^{-2t} + t^3 (-2e^{-2t})$ $\frac{dy}{dt} = 0 \Rightarrow t^2 e^{-2t} (3 - 2t) = 0 \Rightarrow t = \dots$ $t = \frac{3}{2}$ $P\left(2, \frac{27}{8} e^{-3}\right)$	<p><b>M1*</b></p> <p><b>M1dep*</b></p> <p><b>A1</b></p> <p><b>A1</b></p> <p><b>[4]</b></p>	<p><b>2.1</b></p> <p><b>1.1</b></p> <p><b>1.1</b></p> <p><b>2.2a</b></p>	<p>Attempts to differentiate <math>y</math> with respect to <math>t</math> using the product rule – answer of the form <math>\frac{dy}{dt} = \lambda t^2 e^{-2t} + \mu t^3 e^{-2t}</math> or <math>y' = \alpha x^{-5} e^{-6x^{-1}} (\beta x + \gamma)</math></p> <p>Sets their derivative equal to zero and solves for <math>t</math></p> <p>From correct working only (or for <math>x = 2</math>)</p> <p>From correct working only y-coordinate must be exact but ISW</p> <p>Differentiates <math>x</math> with respect to <math>t</math> and attempts to set up integral for the required area</p> <p>Stating 0.5 and 3 is sufficient for this mark</p> <p>Must be correctly shown</p>	<p>Where <math>\lambda, \mu \neq 0</math></p> <p>Where <math>\alpha, \beta, \gamma \neq 0</math></p> <p>Or their <math>\frac{dy}{dx}</math> set = 0 and solve for <math>x</math></p> <p>With <math>\frac{dx}{dt} = kt^{-2}</math> with non-zero <math>k</math></p> <p>If not attempted in (b) then this B mark can be awarded if seen in (c)</p>
5	(b)	$\frac{dx}{dt} = -3t^{-2} \text{ and } \int y \frac{dx}{dt} dt$ $x = 6 \Rightarrow t = 0.5 \text{ and } x = 1 \Rightarrow t = 3$ $\text{Area} = \int_3^{0.5} t^3 e^{-2t} \left(-\frac{3}{t^2}\right) dt = \int_3^{0.5} -3te^{-2t} dt = \int_{0.5}^3 3te^{-2t} dt$	<p><b>M1</b></p> <p><b>B1</b></p> <p><b>A1</b></p> <p><b>[3]</b></p>	<p><b>2.1</b></p> <p><b>1.1</b></p> <p><b>2.2a</b></p>	<p>Differentiates <math>x</math> with respect to <math>t</math> and attempts to set up integral for the required area</p> <p>Stating 0.5 and 3 is sufficient for this mark</p> <p>Must be correctly shown</p>	<p>With <math>\frac{dx}{dt} = kt^{-2}</math> with non-zero <math>k</math></p> <p>If not attempted in (b) then this B mark can be awarded if seen in (c)</p>

5	(c)	$u = 3t, \text{ and } dv \text{ or } \frac{dv}{dt} = e^{-2t}$ $\int 3te^{-2t} dt = -\frac{3}{2}te^{-2t} + \frac{3}{2}\int e^{-2t} dt$ $= \dots -\frac{3}{4}e^{-2t} (+c)$ $\left[-\frac{3}{2}te^{-2t} - \frac{3}{4}e^{-2t}\right]_{0.5}^3 = \left(-\frac{3}{2}(3)e^{-6} - \frac{3}{4}e^{-6}\right) - \left(-\frac{3}{2}(0.5)e^{-1} - \frac{3}{4}e^{-1}\right)$ $\text{Area} = -\frac{21}{4}e^{-6} + \frac{3}{2}e^{-1}$	<p><b>M1*</b></p> <p><b>A1</b></p> <p><b>A1</b></p> <p><b>M1dep*</b></p> <p><b>A1</b></p> <p><b>[5]</b></p>	<p><b>1.1</b></p> <p><b>1.1</b></p> <p><b>1.1</b></p> <p><b>1.1</b></p> <p><b>2.2a</b></p>	<p>Integrating by parts as far as <math>f(t) \pm \int g(t) dt</math></p> <p>Allow correct un-simplified for both A marks</p> <p>Use of their <math>t</math>-limits (so not 1 and 6) in fully integrated expression (must subtract bottom limit from top limit)</p> <p>ISW once correct exact answer seen</p>	<p>Ignore limits for first three marks and allow those who consider <math>-\int 3te^{-2t} dt</math> for possibly full marks</p>
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