

Question		Answer	Marks	AO	Guidance	
8	(a)		M1*	2.1	Differentiates y with respect to x – answer of the form $\pm e^{-2x} \pm \lambda x e^{-2x}$	$\lambda \neq 0$
		$y' = e^{-2x}(1 - 2x)$	A1	1.1		
		$y'' = e^{-2x}(-4 + 4x)$	A1ft	1.1	Follow through their first derivative	
			M1dep*	3.1a	Solves $y'' = 0$ (or attempts to verify $y'' = 0$ by substituting $x = 1$) or considers sign change either side of y''	
		$y'' = 0$ at $x = 1$ and $y''(0.5) = -2e^{-1} < 0$, $y''(1.5) = 2e^{-3} > 0$ (so change of sign indicates a point of inflection at $x = 1$)	A1 [5]	2.2a	Conclusion not required for this mark	
8	(b)		M1*	2.1	Integration by parts – of the form $\pm \alpha x e^{-2x} \pm \beta \int e^{-2x} dx$	Where $\alpha, \beta = 2, \frac{1}{2}$
		$\int x e^{-2x} dx = -\frac{1}{2} x e^{-2x} + \frac{1}{2} \int e^{-2x} dx$	A1	1.1		
		$\int x e^{-2x} dx = -\frac{1}{2} x e^{-2x} - \frac{1}{4} e^{-2x}$	M1dep*	1.1	Use of correct limits in their fully integrated expression – need not be simplified (or equivalent)	
		$\int_0^1 x e^{-2x} dx = \left[-\frac{1}{2} x e^{-2x} - \frac{1}{4} e^{-2x} \right]_0^1$ $= \left(-\frac{1}{2} e^{-2} - \frac{1}{4} e^{-2} \right) - \left(0 - \frac{1}{4} \right)$	A1	1.1	Allow unsimplified	
		$\frac{1}{4} - \frac{3}{4} e^{-2}$	B1	1.1	Or by correctly evaluating $\int_0^1 e^{-2x} dx$	Allow unsimplified
		Area of triangle below $OP = \frac{1}{2} e^{-2}$ $= \frac{1}{4} (1 - 5e^{-2})$	A1 [6]	2.2a	$a = 1, b = -5$ (must be in this form)	