

6

DR

$$\int (2x+9)^{\frac{1}{2}} dx = \frac{1}{3}(2x+9)^{\frac{3}{2}}$$

$$\left[\frac{(2x+9)^{\frac{3}{2}}}{3} \right]_{-\frac{9}{2}}^0 = 9$$

$$4e^{-2x} - 1 = 0 \Rightarrow e^{-2x} = \frac{1}{4}$$

$$-2x = \ln\left(\frac{1}{4}\right)$$

$$x = -\frac{1}{2}\ln\left(\frac{1}{4}\right)$$

$$\int (4e^{-2x} - 1) dx = -2e^{-2x} - x$$

$$\int_0^{\frac{1}{2}\ln 4} (4e^{-2x} - 1) dx = \left(-2e^{-\ln 4} - \frac{1}{2}\ln 4 \right) - (-2)$$

$$\text{Area} = 9 + \frac{3}{2} - \frac{1}{2}\ln 4 = \frac{21}{2} - \frac{1}{2}\ln 4 = \frac{21}{2} - \ln 2$$

M1

A1

A1

M1*

A1

M1*

M1dep*

A1

[8]

2.1

1.1

1.1

3.1a

1.1

1.1

1.1

2.2a

M1 for $k(2x+9)^{\frac{3}{2}}$ with non-zero k

cao (allow unsimplified)

Uses correct limits (or implies correct limits) to get 9. Condone limits the wrong way round leading to -9 but must be changed to $+9$

Attempt to solve $4e^{-2x} - 1 = 0$ by correctly taking logs of both sides leading to $\pm 2x = \pm \ln \alpha$ where $\alpha > 0$

Or equivalent exact value (soi possibly by correct exact value used later)

Integrate $4e^{-2x} - 1$ to obtain $ce^{-2x} \pm x$

Uses limits correctly $F(\frac{1}{2}\ln 4) - F(0)$

(with their $\frac{1}{2}\ln 4$) – **dependent on the previous two M marks** (allow non-exact top limit). Condone limits the wrong way round only if the sign of their answer is subsequently changed

If the values of the integral(s) are changed from negative to positive (e.g. from limits the wrong way round) with no justification given then A0

 $k \neq 1$

Allow sign errors and other minor slips only

e.g. $\frac{1}{2}\ln 4$ or $\ln 2$

Where c is non-zero and $c \neq 4$

If zero limit is assumed to give 0 (with no working) then **M0**

p and q need not be explicitly stated.

$p = \frac{21}{2}$ (oe) and $q = -1$