

Question		Answer	Marks	AO	Guidance	
5	(a)	$\frac{dx}{dt} = 0.2 + \sin t$	B1*	1.1	B1 for $\frac{dx}{dt} = 0.2 \pm \sin t$	
		$\int_0^\pi k \sin^2 t (0.2 + \sin t) dt \Rightarrow$ $\int_0^\pi k(1 - \cos^2 t)(0.2 + \sin t) dt$	M1dep*	3.1a	Uses $\int y \frac{dx}{dt} dt$ and replaces $\sin^2 t$ with $1 - \cos^2 t$ to obtain an expression involving $\cos^2 t$ and $\sin t$	No limits required for this mark
		$k \int_0^\pi (0.2 + \sin t - 0.2 \cos^2 t - \sin t \cos^2 t) dt (=1)$	A1	2.2a	AG (so must be checked carefully for any errors e.g. must contain relevant brackets around the $1 - \cos^2 t$ term(s)) A correct expression e.g. $\int_0^\pi k(1 - \cos^2 t)(0.2 + \sin t) dt$ followed by the correct given answer can score this mark – limits and dt must be seen at least once (but need not be on the final integral)	Do not need to see = 1 anywhere in their solution (and condone lack of brackets around the integrand)
			[3]			

Question		Answer	Marks	AO	Guidance	
5	(b)	$\int (0.2 + \sin t - 0.2(\frac{1}{2})(1 + \cos 2t) - \sin t \cos^2 t) dt$	B1	1.2	Correctly applies $2\cos^2 t \equiv 1 + \cos 2t$ (so not just stating this identity) - implied by seeing $-0.1t - 0.05 \sin 2t$ after integration	e.g. applies could be for an attempt to integrate $\frac{1}{2}(1 + \cos 2t)$ or stating this identity in an integral
		$= 0.2t - \cos t$	B1	1.1	First two terms integrated correctly (Look out for those that have $0.1t$ only from combining $0.2t$ with $-0.1t$)	This mark should be awarded if 0.2 is combined with another constant term and integrated correctly
			M1*	1.1	M1 for an answer of the form $\pm pt \pm q \sin 2t \pm r \cos^3 t$ or an answer of the form $\pm pt \pm q \sin 2t \pm r \sin t \sin 2t \pm u \cos t \cos 2t$ or an answer of the form $\pm pt \pm q \cos t \pm r \sin 2t \pm u \sin t \sin 2t \pm v \cos t \cos 2t$ for non-zero p, q, r (and u, v) from integrating $-0.2 \cos^2 t - \sin t \cos^2 t$	
		$-0.1t - 0.05 \sin 2t + \frac{1}{3} \cos^3 t$	A1	1.1	A1 for the correct remaining three/four terms (Alternatives: $-0.1t - 0.05 \sin 2t + \frac{1}{6} \sin t \sin 2t + \frac{1}{3} \cos t \cos 2t$ or $-0.1t + 0.5 \cos t - 0.05 \sin 2t - \frac{1}{3} \sin t \sin 2t - \frac{1}{6} \cos t \cos 2t$)	
		$\left[0.1t - \cos t - 0.05 \sin 2t + \frac{1}{3} \cos^3 t \right]_0^\pi$ $= (0.1\pi - (-1) - 0 + \frac{1}{3}(-1)^3) - (0 - 1 - 0 + \frac{1}{3})$	M1dep*	1.1	Uses correct limits correctly $F(\pi) - F(0)$ - condone limits the wrong way round only if the sign of their answer is subsequently changed	Must be using exact values (so must include term(s) in π)
		$k(0.1\pi + 2 - \frac{2}{3}) = 1 \Rightarrow k = \frac{30}{3\pi + 40}$	A1	1.1	www oe e.g. $k = \frac{1}{0.1\pi + \frac{4}{3}}$ - isw once a correct expression for k seen	Correct exact value must be seen at some stage for the final mark – check first A mark carefully
			[6]			