

| Question |     | Answer   | Marks   | AOs                                      | Guidance  |  |
|----------|-----|--|---|--|---|--|
| 11       | (a) | <p>The argument is not correct.</p> <p><math>x &lt; 16</math> includes negative values for <math>x</math> for which <math>x^{\frac{1}{2}}</math> does not exist so the statement does not imply that <math>x^{\frac{1}{2}} &lt; 4</math>.</p>  | <p><b>E1</b></p> <p>[1]</p>                                   | 2.3                                      | <p><b>DR</b></p> <p>Allow that <math>x</math> must be positive</p>  | <p>Allow the correct solution <math>0 \leq x &lt; 16</math> or <math>0 &lt; x &lt; 16</math> without further explanation</p> |
| 11       | (b) | <p><b>EITHER</b></p> <p>Take logs of both sides</p> $x \log\left(\frac{1}{2}\right) < \log 4$ <p>Giving <math>x &gt; \frac{\log 4}{\log\left(\frac{1}{2}\right)}</math> [since <math>\log\left(\frac{1}{2}\right)</math> is negative]</p> $x > -2$                                     | <p><b>M1</b></p> <p><b>B1</b></p> <p><b>A1</b></p> <p>[3]</p> | <p>2.1</p> <p><b>1.1a</b></p> <p>2.1</p> | <p><b>DR</b></p> <p>Use of laws of logs must be seen<br/>Allow equivalent with natural logs</p> <p>Award for the boundary value even if only evaluated.<br/>Correct inequality.</p>             |  |
|          |     | <p><b>OR</b></p> <p>Solve <math>\left(\frac{1}{2}\right)^x = 4</math> by taking logs base <math>\frac{1}{2}</math></p> $\log_{\frac{1}{2}}(4) = -2$ <p>Test value – eg when <math>x = 0</math> <math>\left(\frac{1}{2}\right)^0 = 1 &lt; 4</math></p> <p>So <math>x &gt; -2</math></p> | <p><b>M1</b></p> <p><b>B1</b></p> <p><b>A1</b></p> <p>[3]</p> |  | <p><b>DR</b></p> <p>Using log base <math>\frac{1}{2}</math></p> <p>Award for the boundary value even if only seen as part of an equation or incorrect inequality</p> <p>Correct inequality.</p> |  |

| Question |     | Answer  | Marks  | AOs  | Guidance   |   |
|----------|-----|---|--|--|--|---|
| 11       | (c) | <p>Using laws of logs</p> $\log_2(x+8)^2 - \log_2(x+6) = 3$ $\log_2 \frac{(x+8)^2}{(x+6)} = 3$ $\frac{(x+8)^2}{(x+6)} = 2^3$ $(x+8)^2 = 8(x+6)$ $x^2 + 8x + 16 = 0$ <p>Discriminant is <math>8^2 - 4 \times 1 \times 16 = 0</math></p> <p>so there is only one solution</p> | <p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>[5]</b></p> | <p><b>3.1a</b></p> <p><b>3.1a</b></p> <p><b>1.1</b></p> <p><b>2.1</b></p> <p><b>2.2a</b></p> | <p><b>DR</b></p> <p>At least one correct use of laws of logs</p> <p>Clearing logs to obtain <math>2^3</math> or 8 seen in an equation</p> <p>Correct quadratic</p> <p>Attempt to find the discriminant of their quadratic (allow one slip)</p> <p>Correct argument from zero discriminant or repeated root <math>x = -4</math> found</p> | <p>Allow M1 for an attempt to solve their quadratic</p> |