

Question		Answer	Marks	AOs	Guidance	
12	(a)	$\frac{dy}{dx} = 2x - 2x^{-3}$ <p>At $\left(2, \frac{17}{4}\right)$ gradient $= 2 \times 2 - 2 \times 2^{-3} = \frac{15}{4}$</p> <p>Equation of the tangent $y - \frac{17}{4} = \frac{15}{4}(x - 2)$</p> $y = \frac{15}{4}x - \frac{13}{4}$ <p>Crosses x-axis when $y = 0$, $x = \frac{13}{15}$</p> <p>Crosses y-axis when $x = 0$, $y = -\frac{13}{4}$</p> <p>Area of triangle $\frac{1}{2} \times \frac{13}{15} \times \frac{13}{4} = \frac{169}{120}$ [below the axis]</p>	M1 A1 M1 A1 A1 A1 [6]	3.1a 1.1 3.1a 1.1 1.1 1.1	<p>Attempt to differentiate</p> <p>Correct value in any form</p> <p>Using their gradient to find the equation of the tangent</p> <p>Allow 0.867 or better</p> <p>any form</p> <p>FT their values but must be exact. Accept positive or negative value</p>	Note Area 1.41 gets 5/6 marks
12	(b)	<p>At a stationary point $\frac{dy}{dx} = 2x - 2x^{-3} = 0$</p> $x^4 = 1$ giving $x = \pm 1$ so there are only two stationary points $\frac{d^2y}{dx^2} = 2 + 6x^{-4}$ <p>When $x = 1$, $\frac{d^2y}{dx^2} = 2 + 6 \times 1^4 [= 8] > 0$ so minimum point</p> <p>When $x = -1$, $\frac{d^2y}{dx^2} = 2 + 6 \times (-1)^4 [= 8] > 0$ so also minimum point</p> <p>The two stationary points are both minimum points so there is no maximum point.</p>	M1 A1 M1 M1 A1 E1 [6]	1.1a 1.1 1.1a 2.1 2.1 2.2a	<p>Equating their derivative to zero and attempting to solve</p> <p>Finding both roots and no others</p> <p>Differentiating their $\frac{dy}{dx}$</p> <p>Evaluating at (at least one of) their stationary point(s)</p> <p>Argues that both points are minimum from correct working. Allow arguing that second derivative is positive everywhere or a symmetry argument</p> <p>Deduces that there are no maximum points.</p>	<p>Allow for evaluating gradient at appropriate points either side.</p> <p>Arguing point is minimum from their gradients [incl sketch]</p>