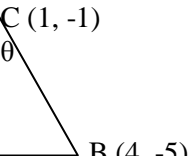


Question		Answer	Marks	AOs	Guidance
12	(i)	C is (1, -1)	<b>B1</b> <b>[1]</b>	<b>1.1a</b>	Cao
	(ii)	A EITHER Substitute $y = \frac{3}{4}x - 8$ into the equation of the circle $(x-1)^2 + \left(\frac{3}{4}x - 8 + 1\right)^2 = 25$ $x^2 - 8x + 16 = 0$ EITHER $(x-4)^2 = 0$ OR Discriminant = $(-8)^2 - 4 \times 1 \times 16 = 0$ So the equation has a repeated root so the line is a tangent	<b>M1</b>  <b>M1</b>  <b>A1</b>  <b>A1</b> <b>[4]</b>	<b>3.1a</b>  <b>1.1a</b>  <b>1.1b</b>  <b>2.2a</b>	<b>AG</b> Attempt to eliminate one variable  Attempt to expand and collect terms to obtain 3 term quadratic expression A correct 3 term quadratic  Clearly argued
	(ii)	A OR Substitute $x = \frac{4}{3}y - \frac{32}{3}$ into the equation of the circle $\left(\frac{4}{3}y - \frac{32}{3} - 1\right)^2 + (y+1)^2 = 25$ $y^2 + 10y + 25 = 0$ EITHER $(y+5)^2 = 0$ OR Discriminant = $10^2 - 4 \times 1 \times 25 = 0$ So the equation has a repeated root so the line is a tangent	<b>M1</b>  <b>M1</b>  <b>A1</b>  <b>A1</b> <b>[4]</b>	<b>3.1a</b>  <b>1.1a</b>  <b>1.1b</b>  <b>2.2a</b>	<b>AG</b> Attempt to eliminate one variable  Attempt to expand and collect terms to obtain 3 term quadratic expression A correct 3 term quadratic  Clearly argued
		B $x = 4$ and $y = -5$ so B is (4, -5)	<b>B1</b> <b>[1]</b>	<b>1.1a</b>	Cao

Question	Answer	Marks	AOs	Guidance	
<b>(iii)</b>	$\angle CAD = \angle CBD = 90^\circ$ (radius is perpendicular to the tangent) Gradient of AC = $\frac{2 - (-1)}{5 - 1} = \frac{3}{4}$ Gradient of BC = $\frac{(-1) - (-5)}{1 - 4} = -\frac{4}{3}$ So AC is perpendicular to BC so $\angle ACB = 90^\circ$ So ADBC is a rectangle Either AC = BC radius [=5] Or AD = BD equal tangents so ADBC is a square.	<b>B1</b>   <b>B1</b>  <b>B1</b> <b>[3]</b>	<b>2.1</b>  <b>3.1a</b>  <b>2.1</b>	Allow for one or other of these angles       Complete proof <b>AG</b>	Allow up to B1, B1 for any two of these three pieces of evidence. Allow the final B1 only when the proof is complete and clearly argued.
	$\angle CAD = \angle CBD = 90^\circ$ (radius is perpendicular to the tangent) Gradient of AC = $\frac{2 - (-1)}{5 - 1} = \frac{3}{4}$ Gradient of BD is $\frac{3}{4}$ So AC is parallel to BD So ADBC is a rectangle AC = BC = radius so ADBC is a square.	<b>B1</b>   <b>B1</b> <b>B1</b>		Allow for one or other of these angles       Complete proof <b>AG</b>	
	$\angle CAD = 90^\circ$ (radius is perpendicular to the tangent) AC = BC radius [=5] Gradient of AC = $\frac{2 - (-1)}{5 - 1} = \frac{3}{4}$ Equation of AD is $y - 2 = -\frac{4}{3}(x - 5)$ So coordinates of D are (8, -2) Hence BD = 5 and AD = 5 So ABCD is a rhombus	<b>B1</b>  <b>B1</b>    <b>B1</b>		Gradient of AD must be found from the coordintes of A and C       Complete proof	

Question	Answer	Marks	AOs	Guidance
(iv)	<p>E is the point (1, -6)</p> <p><b>EITHER</b></p> <p>C (1, -1)</p>  <p>B (4, -5)</p> <p><math>\theta = \arctan\left(\frac{3}{4}\right) = 0.6435</math></p> <p><b>OR</b></p> <p><math>BE = \sqrt{(4-1)^2 + (-5-(-6))^2} = \sqrt{10}</math></p> <p>Cosine rule in triangle BCE</p> <p><math>\cos BCE = \frac{5^2 + 5^2 - 10}{2 \times 5 \times 5} \left[ = \frac{40}{50} \right]</math></p> <p><math>\angle BCE = 0.6435\dots</math></p> <p><b>OR</b></p> <p>M is the midpoint of BE M is (2.5, -5.5)</p> <p><math>BM = \sqrt{(4-2.5)^2 + (-5-(-5.5))^2} = \frac{1}{2}\sqrt{10}</math></p> <p><math>\angle BCM = \arcsin\left(\frac{\frac{1}{2}\sqrt{10}}{5}\right) = 0.32175\dots</math></p> <p><math>\angle BCE = 0.6435\dots</math></p> <p>Area sector = <math>\frac{1}{2}r^2\theta = \frac{1}{2} \times 25 \times 2 \times 0.32175\dots</math></p> <p>= 8.04376</p>	<p><b>B1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>(M1)</b></p> <p><b>(A1)</b></p> <p><b>(M1)</b></p> <p><b>(A1)</b></p> <p><b>M1dep</b></p> <p><b>A1</b></p> <p><b>[5]</b></p>	<p><b>2.1</b></p> <p><b>3.1a</b></p> <p><b>3.1a</b></p> <p><b>3.1a</b></p> <p><b>Using distance BC and the cosine rule</b></p> <p><b>Using trig in triangle BCM or ECM</b></p> <p><b>Allow for <math>\angle BCM</math></b></p> <p><b>Oe. Must be <math>\angle BCE</math></b></p> <p><b>1.1a</b></p> <p><b>1.1b</b></p>	<p>May be implied</p> <p>Right-angled triangle formed and use of arctan</p> <p>oe</p> <p>oe</p> <p>oe</p> <p>Using the sector area formula</p> <p><b>FT their <math>\angle BCM</math></b></p>