

8	(a)	<p>Arithmetic sequence with $a = 9300$ $a_{10} = a + 9d = 9300 + 9d = 3900$ $d = -600$ $a_{20} = a + 19d = 9300 - 19 \times 600 = -2100$ [So 20th term is negative]</p>	<p>M1 A1 A1 [3]</p>	<p>3.1a 1.1b 2.1</p>	<p>Using formula for term of AP with values substituted soi Allow for -2100 without comment</p>	<p>eg $d = 600$ stated but later subtracted Also allow for earlier negative term found and comment that 20th is less</p>
8	(b)	<p>S is increasing as long as the extra terms are positive First negative term when $a_n < 0$ $9300 - 600(n-1) < 0 \Rightarrow \frac{9300}{600} < n-1 \Rightarrow n > 16.5$ So maximum sum after 16 terms $S_{16} = \frac{16}{2}(2 \times 9300 - 600(16-1)) = 76\,800$</p> <p>Alternative solution $S = \frac{n}{2}(2 \times 9300 - 600(n-1)) [= 9600n - 300n^2]$ [To find max S treating S and n as continuous] $\frac{dS}{dn} = 9600 - 600n = 0$ Max sum when $n = 16$ $S_{16} = \frac{16}{2}(2 \times 9300 - 600(16-1)) = 76\,800$</p> <p>Second alternative solution $S_{15} = 76\,500$ $S_{16} = 76\,800$ $S_{17} = 76\,500$ max total is 76800</p>	<p>M1 A1 M1 A1 [4] M1 M1 A1 A1 M1 M1 A1 A1</p>	<p>3.1a 2.2a 1.1a 1.1b</p>	<p>Attempt to find first negative term with 9300 and their d Allow $n > 16$ or $n \geq 17$ oe Using sum with their n and their d cao Using the sum formula with 9300 and their d substituted Setting derivative to zero and solve Allow for $n = 16$ Cao Using the sum formula with 9300 and their d to find at least two totals Evaluating S_{15}, S_{16} and S_{17} Award for S_{16} as maximum identified from correct working Cao</p>	<p>(or last positive term) Also allow M1A1 for establishing $a_{16} = 300$ and $a_{17} = -300$ Also allow M1 for other methods for finding the max A1 for $n = 16$ eg M1A1 for $S_n = k - 300(n-16)^2$ Allow BC FT their d: three consecutive totals around their maximum eg $d = -540$ needs 17th, 18th, 19th totals</p>