

Question		Answer	Marks	AOs	Guidance
12	(a)	$\frac{f(x+h)-f(x)}{h} = \frac{(x+h)^3 - (x+h) - (x^3 - x)}{h}$ $= \frac{x^3 + 3hx^2 + 3h^2x + h^3 - x - h - (x^3 - x)}{h}$ $= \frac{3x^2h + 3xh^2 + h^3 - h}{h} = 3x^2 + 3xh + h^2 - 1$ $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $= \lim_{h \rightarrow 0} (3x^2 - 1 + 3xh + h^2) = 3x^2 - 1$	<b>M1</b>  <b>A1</b>  <b>M1</b>  <b>E1</b> <b>[4]</b>	<b>2.1</b> Substituting into $\frac{f(x+h)-f(x)}{h}$  <b>2.1</b> and attempt to expand $(x+h)^3$  <b>2.1</b> Correct expansion of $(x+h)^3$  <b>2.1</b> Simplifying the fraction to eliminate a denominator  <b>2.1</b> Must include the idea of limit as $h$ tends to zero AG	Allow correct 6 terms not simplified
12	(b)		<b>B1</b>  <b>B1</b> <b>(dep)</b> <b>[2]</b>	<b>1.1a</b> Correct shape with vertex on the negative $y$ -axis <b>1.1</b> $(0, -1)$ labelled and an indication the graph crosses the $x$ -axis at $\left(\pm \frac{1}{\sqrt{3}}, 0\right)$	Allow without $\pm \frac{1}{\sqrt{3}}$ if clear that the points are between $(-1, 0)$ and $(1, 0)$
12	(c)	Point of inflection when $f''(x) = 0$  $f''(x) = 6x = 0$ has only one root $x = 0$ When $x = 0$ , $f'(x) = -1 \neq 0$ so the point of inflection is not a stationary point.	<b>M1</b>  <b>A1</b>  <b>E1</b>  <b>[3]</b>	<b>2.1</b> Equating their second derivative to zero <b>2.1</b> Must explain that this is the only point of inflection <b>2.1</b> Must prove that the point is not stationary from correct value for $f'(0)$	Also allow if shown that the stationary points are at $\left(\pm \frac{1}{\sqrt{3}}, 0\right)$