

Question			Answer	Marks	AOs		Guidance
14	(a)		$h_{\max} = 5.15 + 3.4 \times 1 = 8.55$ $h_{\min} = 5.15 - 3.4 \times 1 = 1.75$ These are the correct h values for high and low tide	B1 [1]	3.4	Choosing $\cos t = \pm 1$ to give both values must be seen Allow without further comment	Allow for using given h values to find $\cos t = \pm 1$ only if there is a comment that these are max and min values for $\cos t$
14	(b)	(i)	When $t = 1$ $8.55 = 5.15 + 3.4 \cos(a + b)$ So $\cos(a + b) = 1$ giving $a + b = 0$	B1 [1]	3.3	Correctly relating high tide, $t = 1$ and $\cos 0$	Accept 8.55 or $\cos t = 1$ as evidence of high tide
14	(b)	(ii)	Minimum when $(a + b) = 180^\circ$ and $t = 7\frac{1}{3}$ So $\frac{22}{3}a + b = 180$	B1 [1]	3.3	Condone the use 7.2 hours here	Allow for $1.75 = 5.15 + 3.4 \cos\left(\frac{22}{3}a + b\right)$
14	(b)	(iii)	Solve simultaneously to give $a = 28.42$ to 2 dp	M1 A1 [2]	3.3 3.3	Attempt to solve simultaneous equations: may be BC AG (value of b not needed here)	$[b = -28.42]$
14	(c)		Substitute $h = 3$ $3 = 5.15 + 3.4 \cos(28.4t - 28.4)$ $\cos(28.4t - 28.4) = -\frac{43}{68}$ $28.4t - 28.4 = 129.2, \quad 230.8$ $t = 5.55, \quad 9.13$ He does not sail between 5.33 am and 9.08 am	M1 A1 A1 [3]	3.4 3.4 3.2a	Attempting to solve trig equation or inequality At least one correct [decimal] value for t Both times correct. Need not convert to hours and minutes. Must indicate between these times	

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14	(d)		EITHER The model predicts every high tide 8.55 m. The next high tide 8.91 is higher than that so not perfect model.	B1 E1 [2]	3.4 3.5b	Allow for a comment about the maximum height being wrong. FT their values
			OR Time difference between high tide and low tide is 6 hr 20 minutes, and between low tide and the next high tide is 5 hours and 40 minutes. The model gives these times as equal, so not perfect model	B1 E1 [2]		Allow for a comment that the time of the next high tide is wrong. FT their values
			OR tide reaches 8.91 m when $\cos(at + b) = 1.105$ which is impossible	B1 E1 [2]		Allow for a comment that the height predicted cannot reach 8.91 m. FT their values
			OR When $t = 12.983$ $h = 8.35$ which is less than the given value of 8.91 m so the model is not suitable	B1 E1 [2]		Allow for $t = 13$ but not $t = 12.59$