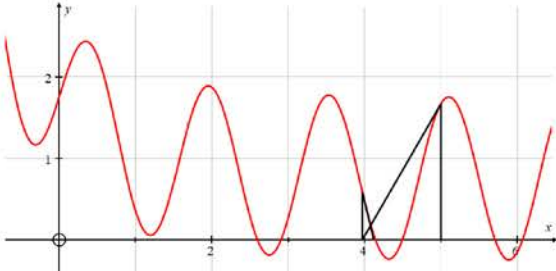


Question			Answer	Marks	AOs	Guidance								
8	(a)		Karim has a valid argument that there is a root between 5 and 6 because there is a change of sign on his table	E1 [1]	2.3	Argues from change of sign that this argument is valid Allow argument is not valid as he does not state that the function is continuous								
8	(b)		There are two roots between 2 and 3 (and/or between 4 and 5) so there is no change of sign in the table	E1 [1]	2.3	Allow for a comment that implies changes of sign are missed								
8	(c)	(i)	$f'(x) = 4 \cos 4x - e^{-x}$ So N-R formula is $x_{n+1} = x_n - \frac{\sin 4x_n + e^{-x_n} + 0.75}{4 \cos 4x_n - e^{-x_n}}$	M1 A1 [2]	1.1b 1.1b	Attempt to differentiate cao, but condone missing subscripts in the fraction								
8	(c)	(ii)	<table border="1" style="display: inline-table; vertical-align: top;"> <tr> <td><math>x_0</math></td> <td>3</td> </tr> <tr> <td><math>x_1</math></td> <td>2.920853...</td> </tr> <tr> <td><math>x_2</math></td> <td>2.908274...</td> </tr> <tr> <td><math>x_3</math></td> <td>2.907846...</td> </tr> </table> <p>The root is 2.908 to 4 s.f.</p>	$x_0$	3	$x_1$	2.920853...	$x_2$	2.908274...	$x_3$	2.907846...	M1 A1 A1 [3]	1.1b 1.1b 2.2a	Produces at least two iterations Three iterations with correct values either rounded or truncated to at least 3 decimal places Correct to at least 3 s.f. FT their values if their sequence seems to converge (root is 2.907845109 to 10 sf)
$x_0$	3													
$x_1$	2.920853...													
$x_2$	2.908274...													
$x_3$	2.907846...													
8	(d)	(i)		B1 B1 [2]	1.1b 1.1b	Attempt to draw a tangent at $x = 5$ as far as the $x$ -axis Drawing the second tangent approximately at the point where $x = 3.97$ as far as the $x$ -axis.								
8	(d)	(ii)	<p>The start value is close to a stationary point, [so the gradient is very small] and the tangent meets the <math>x</math>-axis far away from the required root</p> <p>The sequence converges to a root, but not the required root</p>	B1 B1 [2]	2.4 2.4	Conveys the idea that the stationary point or the value of the gradient causes the problem Conveys the idea that the wrong root is found								
8	(d)	(iii)	Use $x_0$ any value [between 5.28 and 5.85] which is nearer to the required root.	E1 [1]	2.4	Allow for a 'starting value between 5 and 6' oe								