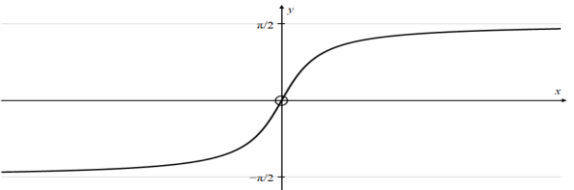


Question		Answer	Marks	AO	Guidance	
3	(a)		B1	1.1b	General shape with horizontal asymptotes Allow if asymptote not drawn provided the intention is clear Must be a one-to-one function	
			B1	1.1b	y-values $\pm \frac{\pi}{2}$ seen	
			[2]			
3	(b)	<p>DR</p> <p>Graphs intersect when $3\sin x \cos x = \cos^2 x$ Either $\cos x = 0$ giving $x = -\frac{\pi}{2}, \frac{\pi}{2}$ or $3\sin x = \cos x$ giving $\tan x = \frac{1}{3}$ $x = 0.322, x = -2.82$ to 3s.f.</p> <p>When $x = 0.322$ or $x = -2.82$ $y = 0.9$ [So the points of intersection are $(0.322, 0.9), (-2.82, 0.9), (-\frac{\pi}{2}, 0), (\frac{\pi}{2}, 0)$]</p>	M1	1.1a	soi	
			M1	1.1b	Attempt to solve $\cos x = 0$	
			A1	2.1	Both values in radians needed	
			M1	2.1		Allow for $x = \tan^{-1} \frac{1}{3}$
			A1	2.1	Both values in radians to at least 2 s.f. needed. Do not award if additional values inside the interval $[-\pi, \pi]$ Ignore additional values outside the interval $[-\pi, \pi]$.	SC1 award for 18.4° and -161.6° if 90° already seen
			A1	2.1	Allow awrt 0.90	Notice 0.9 is exact.
			[6]			

Alternative method

DR

Graphs intersect when $3\sin x \cos x = \cos^2 x$

Either $\cos x = 0$

giving $x = -\frac{\pi}{2}, \frac{\pi}{2}$

Or $3\sin x = \cos x$

Squaring gives

$$9\sin^2 x = \cos^2 x = 1 - \sin^2 x$$

$$10\sin^2 x = 1$$

$$\sin x = \pm\sqrt{0.1}$$

$$x = -2.820, -0.322, 0.322, 2.820$$

Select genuine roots 0.322, -2.820

When $x = 0.322$ or $x = -2.82$ $y = 0.9$

[So the points of intersection are

$$\left(-\frac{\pi}{2}, 0\right), \left(\frac{\pi}{2}, 0\right), (0.322, 0.9), (-2.820, 0.9)]$$

M1

M1

A1

1.1b

2.1

soi

Attempt to solve $\cos x = 0$

Both values in radians needed

M1

A1

A1

2.1

Complete method for finding at least one value for $\sin x$

Both correct roots and no others in the range

Allow awrt 0.90

Notice 0.9 is exact.

[6]