

Question	Answer	Marks	AO	Guidance
11	<p>Let $u = 2x + k$ $2dx = du$</p> $\int \frac{2}{(2x+k)^2} dx = \int \frac{1}{u^2} du$ $= -\frac{1}{u} [+c]$ $\int_k^{2k} \frac{2}{(2x+k)^2} dx = \int_{3k}^{5k} \left(\frac{1}{u^2}\right) du = -\frac{1}{5k} + \frac{1}{3k}$ <p>Alternatively, by inspection</p> $\int_k^{2k} \frac{2}{(2x+k)^2} dx = \left[-(2x+k)^{-1} \right]_k^{2k}$ $= -\frac{1}{5k} + \frac{1}{3k}$ $= \frac{2}{15k}$ <p>This is inversely proportional to k [with constant of proportionality $\frac{2}{15}$]</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A2</p> <p>M1</p> <p>A1</p> <p>E1</p> <p>[6]</p>	<p>2.1</p> <p>2.1</p> <p>2.1</p> <p>2.1</p> <p>2.1</p> <p>2.1</p> <p>2.1</p> <p>2.1</p> <p>2.2a</p>	<p>Substituting $u = 2x + k$ Allow for a different substitution giving an integral in u only Ignore limits</p> <p>Correct integrand in terms of u Ignore limits</p> <p>correct indefinite integral constant need not be seen</p> <p>substituting correct new limits into their integrated expression, or substituting in terms of x and using original limits</p> <p>Integrating by inspection to obtain any multiple of $(2x + k)^{-1}$</p> <p>Fully correct indefinite integral – need not be simplified. substituting limits into their integrated expression</p> <p>Allow $\left(-\frac{1}{5} + \frac{1}{3}\right)\frac{1}{k}$ seen</p> <p>FT their definite integral Must use phrase “inversely proportional” to k or indicates $\propto \frac{1}{k}$</p> <p>Allow for $\int \frac{a}{u^2} du$ for any constant seen</p> <p>Allow if $\frac{a}{k}$ required at the start of the argument</p>