

Question		Answer	Marks	AO	Guidance
10	(a)	$(x - 2) = 5\cos\theta$ and $(y - 1) = 5\sin\theta$  $(x - 2)^2 + (y - 1)^2 = (5\cos\theta)^2 + (5\sin\theta)^2$ <b>oe</b>  $(x - 2)^2 + (y - 1)^2 = 5^2$ <b>oe isw</b>  <b>or</b> $\frac{(x-2)^2}{5^2} + \frac{(y-1)^2}{5^2} = 1$ <b>oe isw</b>	<b>M1</b>  <b>M1</b>  <b>A1</b>	<b>3.1a</b>  <b>1.1</b>  <b>1.1</b>	allow sign errors  <b>or</b> $\left(\frac{x-2}{5}\right)^2 + \left(\frac{y-1}{5}\right)^2 = \cos^2\theta + \sin^2\theta$ <b>oe</b>  may see eg $x^2 - 4x + y^2 - 2y = 20$ if <b>M0M0</b> allow <b>SC1</b> for  $y = 1 + 5\sin\left(\cos^{-1}\left(\frac{x-2}{5}\right)\right)$  or $x = 2 + 5\cos\left(\sin^{-1}\left(\frac{y-1}{5}\right)\right)$
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		<i>Alternatively</i> $x^2 = (2 + 5\cos\theta)^2$ and $y^2 = (1 + 5\sin\theta)^2$  $x^2 + y^2 = 5 + 20\cos\theta + 10\sin\theta + 25\sin^2\theta + 25\cos^2\theta$  $x^2 + y^2 = 20 + 4x + 2y$ <b>oe isw</b>	<b>M1</b>  <b>M1</b>  <b>A1</b>		if only seen in expanded form, allow one coefficient error; allow sign errors must have terms in $\cos\theta$ and $\sin\theta$
		<i>Alternatively</i> radius = 5 and centre is (2, 1)  $(x - 2)^2 + (y - 1)^2 = 5^2$	<b>M1</b>  <b>M1</b> <b>A1</b>		allow sign error in coordinates of centre  <b>FT</b> their centre all correct

Question		Answer	Marks	AO	Guidance
10	(b)	<p>gradient of radius is <math>\frac{-4}{3}</math></p> <p>gradient of tangent is <math>\frac{3}{4}</math></p> <p><math>(y - -3) = \frac{3}{4}(x - 5)</math> <b>oe</b></p> <p><math>3x - 4y - 27 = 0</math> <i>or</i> <math>-3x + 4y + 27 = 0</math></p>	<p><b>B1</b></p> <p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1</b></p>	<p><b>3.1a</b></p> <p><b>2.1</b></p> <p><b>2.4</b></p> <p><b>1.1</b></p>	<p><b>FT</b> 1 ÷ <i>their</i> <math>-\frac{4}{3}</math></p> <p>allow one sign error; <b>FT</b> <i>their</i> <math>\frac{3}{4}</math></p> <p>may see <math>-3 = \frac{3}{4} \times 5 + c</math></p>
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		<p><i>Alternatively</i></p> <p><math>\frac{dy}{dx} = \frac{5\cos\theta}{-5\sin\theta}</math> <b>oe</b></p> <p>substitution of <math>\cos\theta = \frac{3}{5}</math> and <math>\sin\theta = -\frac{4}{5}</math> <b>oe</b></p> <p><b>or</b> (5,-3) in their <math>\frac{dy}{dx}</math></p> <p><math>(y - -3) = \frac{3}{4}(x - 5)</math> <b>oe</b></p> <p><math>3x - 4y - 27 = 0</math> <i>or</i> <math>-3x + 4y + 27 = 0</math></p>	<p><b>B1</b></p> <p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1</b></p>		<p><b>or</b> <math>\frac{dy}{dx} = \frac{2-x}{y-1}</math> <b>oe</b></p> <p>eg <math>2(x - 2) + 2(y - 1)\frac{dy}{dx} = 0</math></p> <p><math>\frac{dy}{dx} = \frac{3/5}{-(-4/5)}</math> <b>or</b> <math>\frac{2-5}{-3-1}</math> <b>oe</b>; allow one sign error;</p> <p>allow one sign error; <b>FT</b> <i>their</i> <math>\frac{3}{4}</math></p> <p>may see <math>-3 = \frac{3}{4} \times 5 + c</math></p>
			[4]		