

Question		Answer	Marks	AO	Guidance
15	(a) (i)	337	B1	1.1	
			[1]		
15	(a) (ii)	$\sqrt{\frac{1}{54} (6247066.6 - 55 \times 337^2)}$ ≈ 3.78	B1	1.1	<p>NB $\sqrt{14.289} = 3.7800 \dots$</p> <p>may see $\sqrt{\frac{6247066.6}{55} - 337^2} \times \sqrt{\frac{55}{54}}$ or $\sqrt{\frac{6247066.6}{54} - \frac{55 \times 337^2}{54}}$ oe;</p> <p>AG must see substitution of at least three of 6247066.6, 337, 55 and 54</p>
			[1]		

Question		Answer	Marks	AO	Guidance
15	(b)	allow any two reasons	E1	2.4	
		eg distribution is (approximately) symmetrical	E1	2.2b	
		eg distribution is (approximately) bell-shaped			
		eg distribution is unimodal			
		eg data is continuous			
			[2]		
15	(c)	P($X < 330$) found from N(their 337, 3.78 ²)	M1	3.3	may be implied by 0.032; allow a more precise value for 3.78 if found in part (a)(ii)
					NB eg N(-9E999,330,337,3.78);
		100 × their 0.032	M1	3.4	NB may see $\sigma^2 = \frac{643}{45}$ or $z = \frac{330-337}{3.78} (= -1.85 \dots)$
		awrt 3.2 www	A1	1.1	mark the final answer
			[3]		
15	(d)	($z =$) $\pm 2.3263 \dots$ seen	B1	3.1a	to 2 or more dp
		their $z = \frac{330-\mu}{3.78}$	M1	2.1	
		338.79 \approx 339	A1	3.2a	must be correct to 3 sf
					A0 for $\mu \geq 339$ or $\mu > 339$
			[3]		

Question		Answer	Marks	AO	Guidance
15	(d)	<p><i>Alternatively using calculator</i></p> <p>eg $\text{cdfNormal}(-9.999 \times 10^{999}, 330, 338, 3.78)$ $= 0.017(155\dots) > 0.01$</p> <p>or</p> <p>eg $\text{cdfNormal}(-9.999 \times 10^{999}, 330, 338.5,$ $3.78) = 0.012(266\dots) > 0.01$</p> <p>eg $\text{cdfNormal}(-9.999 \times 10^{999}, 330, 339, 3.78)$ $= 0.0086(339\dots) < 0.01$</p> <p>hence minimum value for μ is 339</p>	M1		<p>allow slip in calculation if intent is clear; allow for any value between 338 and 338.78 inclusive</p> <p>must see correct distributions if probabilities are wrong</p>
		M1		<p>allow for any value between 338.8 and 339.5</p> <p>NB critical value is 338.79</p>	
		A1		<p>must be correct to 3 sf; A0 for $\mu \geq 339$ or $\mu > 339$</p>	
		3			

15	(e)	<p>$H_0: \mu = 340$ $H_1: \mu < 340$</p> <p>μ is the population mean (volume of drink in a bottle of Fizzipop)</p> <p>$N\left(340, \frac{3.78^2}{100}\right)$ oe seen</p> <p>$[P(\bar{X} < 339.37) =]0.0477 - 0.048$</p> <p>their 0.048 correctly compared with 0.05</p> <p>do not accept H_0 or reject H_0 or accept H_1 or significant</p> <p>there is sufficient evidence at the 5% level to suggest that the mean volume of drink in a bottle of Fizzipop is less than 340 ml oe</p>	<p>B1</p> <p>B1</p> <p>M1*</p> <p>A1</p> <p>M1dep*</p> <p>A1FT</p> <p>A1</p> <p>[7]</p>	<p>1.1</p> <p>2.5</p> <p>3.3</p> <p>3.4</p> <p>3.4</p> <p>1.1</p> <p>3.5a</p>	<p>do not allow \bar{X} or X, but allow other symbol if defined as [population] mean volume; allow equivalent in words</p> <p>may be implied by $0.0477 - 0.048$</p> <p>may see $N(340, 0.378^2)$ may see $\sigma^2 = \frac{643}{4500}$</p> <p>allow slip such as X for \bar{X} but do not allow μ</p> <p>dependent on award of all other marks apart from second B1 do not allow eg conclude / prove / indicate or other assertive statement instead of suggest</p>
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15	(e)	<p>Alternatively $H_0: \mu = 340$ $H_1: \mu < 340$</p> <p>μ is the population mean (volume of drink in a bottle of Fizzipop)</p> <p>$N\left(340, \frac{3.78^2}{100}\right)$ oe seen</p> <p>[critical region is $\bar{X} <]339.378 - 339.38$</p> <p>339.37 correctly compared with their 339.378</p> <p>do not accept H_0 or reject H_0 or accept H_1 or significant</p> <p>there is sufficient evidence at the 5% level to suggest that the mean volume of drink in a bottle of Fizzipop is less than 340 ml oe</p>	<p>B1</p> <p>B1</p> <p>M1*</p> <p>A1</p> <p>M1dep*</p> <p>A1FT</p> <p>A1</p> <p>[7]</p>	<p>1.1</p> <p>2.5</p> <p>3.3</p> <p>3.4</p> <p>3.4</p> <p>1.1</p> <p>3.5a</p>	<p>do not allow \bar{X} or X, but allow other symbol if defined as [population] mean volume allow equivalent in words</p> <p>may be implied by $339.378 - 339.38$</p> <p>may see $N(340, 0.378^2)$</p> <p>may see $\sigma^2 = \frac{643}{4500}$</p> <p>or [critical value is $\bar{X} =]339.378 - 339.38$; allow slip such as X for \bar{X} but do not allow μ</p> <p>allow eg so 339.37 is in the critical region if critical region explicitly identified</p> <p>A0 if $339.37 >$ their 339.378</p> <p>dependent on award of all other marks apart from second B1 do not allow eg conclude / prove / indicate or other assertive statement instead of suggest</p>
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15	(e)	<p><i>Alternatively, using standard Normal distribution</i></p> <p>$H_0: \mu = 340$ $H_1: \mu < 340$</p> <p>μ is the population mean (volume of drink in a bottle of Fizzipop)</p> <p>$N\left(340, \frac{3.78^2}{100}\right)$ oe seen</p> <p>[z =] - 1.667</p> <p>their z correctly compared with - 1.64485 to 2 or more dp oe; must come from $N(340, \sigma)$</p> <p>do not accept H_0 or reject H_0 or accept H_1 or significant</p> <p>there is sufficient evidence at the 5% level to suggest that the mean volume of drink in a bottle of Fizzipop is less than 340 ml oe</p>	<p>B1</p> <p>B1</p> <p>M1*</p> <p>A1</p> <p>M1dep*</p> <p>A1FT</p> <p>A1</p>	<p>do not allow \bar{X} or X, but allow other symbol if defined as [population] mean volume allow equivalent in words</p> <p>may be implied by $z = -1.667$</p> <p>may see $N(340, 0.378^2)$</p> <p>may see $\sigma^2 = \frac{643}{4500}$</p> <p>A0 if their $z > -1.64485$</p> <p>dependent on award of all other marks apart from second B1 do not allow eg conclude / prove / indicate or other assertive statement instead of suggest</p>
			[7]	