

Question			Answer	Marks	AOs	Guidance	
8	(a)	(i)	$\frac{dy}{dx} = \frac{-4x}{(x^2 + 1)^3}$ $\frac{d^2y}{dx^2} = \frac{-4(x^2+1)^3 + 4x \cdot 2x \cdot 3(x^2+1)^2}{(x^2+1)^6}$ $\frac{d^2y}{dx^2} = \frac{-4(x^2 + 1) + 24x^2}{(x^2 + 1)^4}$ $\Rightarrow \frac{d^2y}{dx^2} = \frac{20x^2 - 4}{(x^2 + 1)^4}$	<b>M1</b>  <b>A1</b>  <b>M1</b>  <b>A1</b>  <b>A1</b>	<b>1.1a</b>  <b>1.1</b>  <b>1.1a</b>  <b>1.1</b>  <b>2.1</b>	Attempt to differentiate  Correct first derivative  Attempt to use quotient rule to find second derivative Any correct expression for second derivative  Simplifying expression for second derivative by cancelling $(x^2 + 1)$ and correct completion (AG)	chain or quotient or product rule Don't have to simplify  For each M1 allow one error
8	(a)	(ii)	<b>DR</b> For concave downwards, $\frac{20x^2-4}{(x^2+1)^4} < 0$ so $20x^2 - 4 < 0$ $5x^2 < 1$ so $x^2 < \frac{1}{5}$ $-\frac{1}{\sqrt{5}} < x < \frac{1}{\sqrt{5}}$	<b>M1</b>  <b>M1</b>  <b>A1</b>  <b>[3]</b>	<b>2.2a</b>  <b>1.1</b>  <b>2.5</b>	Or $x = \pm \frac{1}{\sqrt{5}}$  Correct solution correctly expressed	Condone $x^2 > \frac{1}{5}$ following $y'' > 0$ for M1  Allow decimals ( $\pm 0.447$ )

Question		Answer	Marks	AOs	Guidance	
8	(b)	$\frac{dx}{d\theta} = \sec^2 \theta$ $\int_{x=-1}^{x=1} \frac{\sec^2 \theta}{(1 + \tan^2 \theta)^2} d\theta$ $\int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \frac{\sec^2 \theta}{(1 + \tan^2 \theta)^2} d\theta$ $\int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \frac{1}{\sec^2 \theta} d\theta$ $\int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \cos^2 \theta d\theta$ $\int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \frac{1}{2} (\cos 2\theta + 1) d\theta$ $\frac{1}{2} \left[ \frac{1}{2} \sin 2\theta + \theta \right]_{-\frac{\pi}{4}}^{\frac{\pi}{4}}$ $\frac{1}{2} \left( 1 + \frac{\pi}{2} \right) = \frac{1}{2} + \frac{\pi}{4}$	<b>M1</b>  <b>M1</b>  <b>M1</b>  <b>M1</b>  <b>M1</b>  <b>M1</b>	<b>1.1a</b>  <b>1.1</b>  <b>1.1</b>  <b>2.2a</b>  <b>1.1</b>  <b>3.1a</b>  <b>1.1</b>  <b>2.1</b>	o.e.  Substitution for either $x$ or $dx$ (limits may be missing)  Limits (may be done at any point)  Use of $1 + \tan^2 \theta = \sec^2 \theta$  Use of $\sec \theta = \frac{1}{\cos \theta}$  Use of $\cos 2\theta = 2 \cos^2 \theta - 1$  Integration. Must include at least one trig term. Limits may be wrong or missing  Exact form	Condone $\sec^2 x$
			<b>[8]</b>			