

3	(a)	1	B1 [1]	2.2a	Cao Must be clear that the limit is equal to 1 . Therefore tending to or approaching 1 or 0.999 or $\rightarrow 1$ etc do not score
3	(b)	$a_n = 1 - \frac{1}{n+1}$ <p>$n+1$ increases as n increases so $\frac{1}{n+1}$ decreases Less is being taken away from 1 each time so $a_n = 1 - \frac{1}{n+1}$ increases</p>	M1 M1 E1	3.1a 2.4 2.1	<p>Convincing explanation that $\frac{1}{n+1}$ decreases</p> <p>Convincing completion (A.G.)</p> <p>Special Case (Max 2 for this method) Correct differentiation and states > 0 to demonstrate increasing SC B1 Goes on to consider [positive] integers as a subset of reals to complete their argument SC B1 dep on first B1.</p>
			[3]		

Alternative method 1

$$\frac{n+1}{n+2}$$

$$n(n+2) < (n+1)^2$$

$$n(n+2) = n^2 + 2n \text{ and } (n+1)^2 = n^2 + 2n + 1$$

Expanding brackets to give convincing completion (A.G.)

M1

This method is testing $\frac{n}{n+1} < \frac{n+1}{n+2}$

Formulating expression for (n+1)th or (n-1)th term

M1

For formulating inequality and cross multiplying

E1

Probably see $\frac{n+1}{n+2} > \frac{n}{n+1}$ [i.e. increasing]

Alternative method 2

$$\frac{n+1}{n+2}$$

$$\text{Difference is } \frac{n+1}{n+2} - \frac{n}{n+1} = \frac{(n+1)^2 - n(n+2)}{(n+1)(n+2)}$$

$$\frac{(n+1)^2 - n(n+2)}{(n+1)(n+2)} = \frac{1}{(n+1)(n+2)} > 0$$

So sequence is increasing

M1

Formulating expression for (n+1)th term

M1

Finding difference and attempts to form a single fraction
eg may be $a_n - a_{n+1}$

E1

Convincing completion (A.G.)