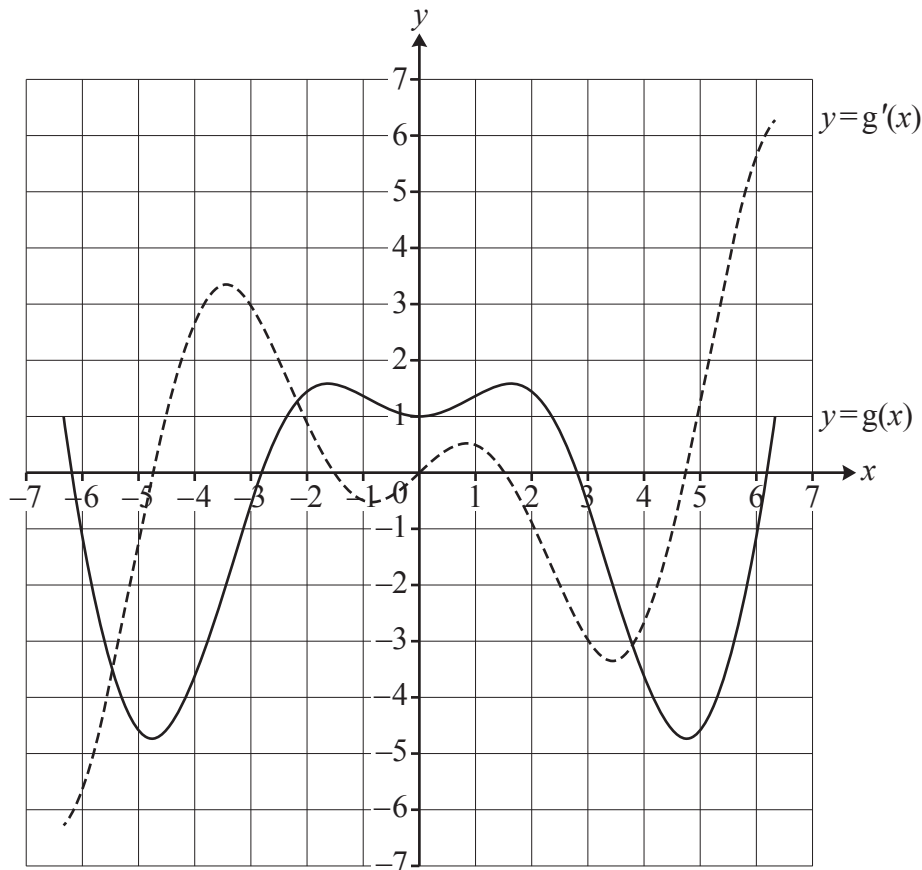


- 11 Fig. 11.1 shows the curve with equation $y = g(x)$ where $g(x) = x \sin x + \cos x$ and the curve of the gradient function $y = g'(x)$ for $-2\pi \leq x \leq 2\pi$.

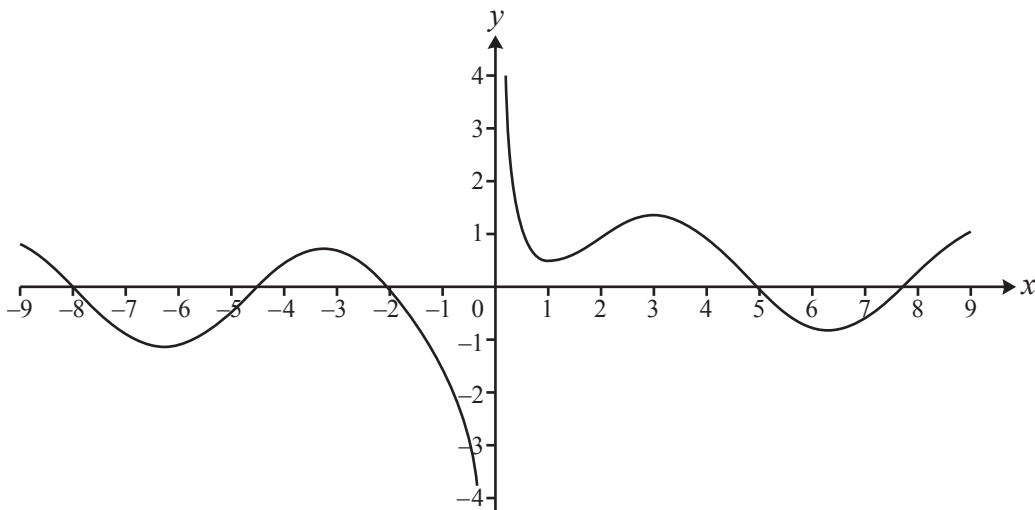
Fig. 11.1



- (a) Show that the x -coordinates of the points on the curve $y = g(x)$ where the gradient is 1 satisfy the equation $\frac{1}{x} - \cos x = 0$.

Fig. 11.2 shows part of the curve with equation $y = \frac{1}{x} - \cos x$.

Fig. 11.2



- (b) Use the Newton-Raphson method with a suitable starting value to find the smallest positive x -coordinate of a point on the curve $y = x \sin x + \cos x$ where the gradient is 1.

You should write down at least the following.

- The iteration you use
- The starting value
- The solution correct to 4 decimal places

[4]

- (c) Explain why $x_1 = 3$ is **not** a suitable starting value for the Newton-Raphson method in part (b).

[1]